## The Flow of Information RTDM Bootcamp on Power Systems: Lecture 2 January 22–26, 2018

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Based in part on joint research with Dr. Y. Chen UF/NREL, J. Mathias, P. Barooah, UF & A. Bušić, Inria

Thanks to to our sponsors: NSF, Google, DOE, ARPA-E

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My own: stochastic processes and control ...



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 $\bullet$  My own: stochastic processes and control ...



• 15 years ago: with economist In-Koo Cho

Can we understand the California power crisis?



• My own: stochastic processes and control ...



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Can we understand the California power crisis? 2003: Dynamics of ancillary service prices in power distribution systems

**Background** 

• My own: stochastic processes and control ...

• 15 years ago: with economist In-Koo Cho

Can we understand the California power crisis? 2003: Dynamics of ancillary service prices in power distribution systems

"... earlier book with Tweedie is the bible for economists ..." –Thomas Sargent, NYU, as president of AEA







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- Stay tuned for Zap Q-Learning in March!メロト メ都 トメ 君 トメ 君 トー  $299$

"... earlier book with Tweedie is the bible for economists ..." –Thomas Sargent, NYU, as president of AEA



focus on distributed control with Barooah & Bušić and our students

• 15 years ago: with economist In-Koo Cho

• Today, among other things,





My own: stochastic processes and control ...

**Background** 

### <span id="page-6-0"></span>The Flow of Information **Outline**



1 [Information Signals](#page-7-0)

2 [Distributed Control Today](#page-34-0)

3 [Virtual Energy Storage](#page-60-0)

#### **[Conclusions](#page-110-0)**





<span id="page-7-0"></span>

### Information Signals

<span id="page-8-0"></span>



 $\mathbf{A} \equiv \mathbf{A} + \mathbf{A} \mathbf{B} + \mathbf{A} \mathbf{B} + \mathbf{A} \mathbf{B} + \mathbf{B} \mathbf{B}$ 





Home > About Us > Our Business > The ISO grid

#### The ISO grid

The ISO manages the flow of electricity for about 80 percent of California and a small part of Nevada, which encompasses all of the investor-owned utility territories and some municipal utility service areas. There are some pockets where local public power companies manage their own transmission systems.

The ISO is the largest of about 38 balancing authorities in the western interconnection, handling an estimated 35 percent of the electric load in the West. A balancing authority is responsible for operating a transmission control area. It matches generation with load and maintains consistent electric frequency of the grid, even during extreme weather conditions or natural disasters.

<span id="page-9-0"></span>Balancing frequency and tie-line error

#### Frequency deviation of 0.1 Hz  $\implies$  Panic!



Breaker failure  $\implies$  transients  $\implies$  two generators tripped

<span id="page-10-0"></span>Balancing frequency and tie-line error

#### Frequency is continuous across interconnected regions

#### **FNET/GridEye Web Display**



<span id="page-11-0"></span>Balancing frequency and tie-line error

#### Phase angle is also continuous

#### **FNET/GridEye Web Display**



<span id="page-12-0"></span>Balancing frequency and tie-line error

#### Frequency floats more freely in other regions of the globe



A disturbance in Agra appears to spread instantly to Mumbai and Calcutta.

<span id="page-13-0"></span>Ducks, Peaks, Ramps, Voltage, Power, Energy ...

#### **•** Afternoon peaks in New York



http://www.nyiso.com/public/markets\_operations/market\_data/graphs/index.jsp

<span id="page-14-0"></span>Ducks, Peaks, Ramps, Voltage, Power, Energy ...

#### **• Dreaded Duck Curve in the South West**



Net demand (demand minus solar and wind) AS OF 16:40

This graph illustrates how the ISO meets demand while managing the quickly changing ramp rates of variable energy resources, such as solar and wind. Learn how the ISO maintains reliability while maximizing clean energy sources.

 $\mathbf{E} = \mathbf{A} \oplus \mathbf{A} + \mathbf{A} \oplus \mathbf{A} + \mathbf{A} \oplus \mathbf{A} + \mathbf{A} \oplus \mathbf{A}$ 

<span id="page-15-0"></span>Ducks, Peaks, Ramps, Voltage, Power, Energy ...

#### **• Dreaded Duck Curve in the South West**



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<span id="page-16-0"></span>Ducks, Peaks, Ramps, Voltage, Power, Energy ...

#### • Wind in the North West



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<span id="page-17-0"></span>Ducks, Peaks, Ramps, Voltage, Power, Energy ...

#### Wind and Sun in Germany





<span id="page-18-0"></span>Engineering & Markets : Midcontinent ISO on a typical fall morning



[https://www.misoenergy.org/LMPContourMap/MISO\\_All.html](https://www.misoenergy.org/LMPContourMap/MISO_All.html)  $6/56$ 

<span id="page-19-0"></span>Engineering & Markets : Midcontinent ISO on a typical fall morning



[https://www.misoenergy.org/LMPContourMap/MISO\\_All.html](https://www.misoenergy.org/LMPContourMap/MISO_All.html)  $\begin{array}{rcl} \mathbb{R} & \rightarrow & \mathbb{R} & \rightarrow & \mathbb{R} & \Rightarrow & \mathbb{R} & \mathbb{R} \times \mathbb{R} \\ 6 & / 56 & & & \end{array}$ 

<span id="page-20-0"></span>Engineering & Markets : CAISO yesterday noon



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<span id="page-21-0"></span>Engineering & Markets : ERCOT yesterday afternoon



 $Normal Gradient$   $A \cup B \cup AB \cup AB \cup AB \cup AB \cup BA$ 

<span id="page-22-0"></span>Engineering & Markets : ERCOT yesterday afternoon



High Gradient  $\overline{B}$   $\overline{B}$ 

<span id="page-23-0"></span>Engineering & Markets : ERCOT scarcity pricing



### <span id="page-24-0"></span>Why is the BA so picky about  $\omega$ ?

Why should the generators care?



1,200MW plant in Florida

 $\bullet$  $\bullet$  $\bullet$  U.S. CC Gas-turbine generators: most effic[ien](#page-23-0)[t a](#page-25-0)[n](#page-27-0)[d](#page-24-0) [e](#page-27-0)[x](#page-23-0)[p](#page-24-0)en[si](#page-6-0)[v](#page-7-0)e

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## <span id="page-25-0"></span>Why is the BA so picky about  $\omega$ ?

Why should the generators care?

- U.S. CC Gas-turbine generators: most efficient and expensive
- Powerful, but dainty!



Generator designed to "trip" if  $\omega$  is slightly out of bounds

## <span id="page-26-0"></span>Why is the BA so picky about  $\omega$ ?

Why should the generators care?

- U.S. CC Gas-turbine generators: most efficient and expensive
- Powerful, but dainty!



Generator designed to "trip" if  $\omega$  is slightly out of bounds

Punished with droop, AGC, ramping services, weeks with steady wind ...

 $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right.$ 

<span id="page-27-0"></span>Take the Quality of Life (QoL) Test: How Did You Feel When a Stranger...

<span id="page-28-0"></span>Take the Quality of Life (QoL) Test: How Did You Feel When a Stranger...



<span id="page-29-0"></span>Take the Quality of Life (QoL) Test: How Did You Feel When a Stranger...



Response of a typical rational agent

<span id="page-30-0"></span>Take the Quality of Life (QoL) Test: How Did You Feel When a Stranger...

- Unplugged your
- · Fridge
- · Water heater
- · Pool pump (one million in CA)



<span id="page-31-0"></span>Take the Quality of Life (QoL) Test: How Did You Feel When a Stranger...

- Unplugged your
- 
- · Fridge<br>• Water heater



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Not so upsetting

<span id="page-32-0"></span>Take the Quality of Life (QoL) Test: How Did You Feel When a Stranger...



Not so upsetting

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Flexible loads are not dispensable loads:

<span id="page-33-0"></span>Take the Quality of Life (QoL) Test: How Did You Feel When a Stranger...



Not so upsetting

Flexible loads are not dispensable loads: power can be shifted thanks to

- **o** thermal inertia
- **•** time-constants of algae

Each is a form of storage

<span id="page-34-0"></span>

### Distributed Control Today

### <span id="page-35-0"></span>Comparison: Flight control Distributed Control



Local control loops located at elevators, flaps, ailerons
## <span id="page-36-0"></span>Comparison: Flight control Distributed Control



Local control loops located at elevators, flaps, ailerons

Resulting input-output behavior is nearly linear, and highly predictable

## <span id="page-37-0"></span>Comparison: Flight control Distributed Control



Local control loops located at elevators, flaps, ailerons

Resulting input-output behavior is nearly linear, and highly predictable  $\implies$  Simplifies global control

### <span id="page-38-0"></span>Comparison: Flight control Distributed Control



<span id="page-39-0"></span>Crash course on Droop and AGC

#### **Don't forget:** [Yesterday's tutorial by R. Murray, Caltech](https://simons.berkeley.edu/talks/murray-control-1)



<span id="page-40-0"></span>Crash course on Droop and AGC

#### Don't forget:

<span id="page-41-0"></span>Crash course on Droop and AGC

#### **Don't forget:** Frequency is continuous across interconnected regions



#### **FNET/GridEye Web Display**

## <span id="page-42-0"></span>Grid Control Architecture Crash course on Droop and AGC

Distributed Control Description in Three Steps:

Each generator measures system frequency **Primary control loop**: adjusts valve position in response to deviation



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<span id="page-43-0"></span>Crash course on Droop and AGC

#### Distributed Control Description in Three Steps:



<span id="page-44-0"></span>Crash course on Droop and AGC

#### Distributed Control Description in Three Steps:



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<span id="page-45-0"></span>Crash course on Droop and AGC



Questions:

- Why this architecture?
- How to model the aggregate input-output system:

$$
\text{AGC}(t) \longrightarrow \omega(t)
$$

<span id="page-46-0"></span>Crash course on Droop and AGC



Questions:

- Why this architecture?
- How to model the aggregate input-output system:

$$
\text{AGC}(t) \longrightarrow \omega(t)
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Answer is similar to the airplane:

local control shapes aggregate dynamics so Grid is more easily controlled

<span id="page-47-0"></span>Crash course on Droop and AGC

Answer is similar to the airplane: local control shapes the aggregate so it is more easily controlled.

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Example from  $[4, 22, 15]$  $[4, 22, 15]$  $[4, 22, 15]$  (general theory in  $[5]$ ):



<span id="page-48-0"></span>Crash course on Droop and AGC

Answer is similar to the airplane: local control shapes the aggregate so it is more easily controlled.

Example from  $[4, 22, 15]$  $[4, 22, 15]$  $[4, 22, 15]$  (general theory in  $[5]$ ):



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<span id="page-49-0"></span>Crash course on Droop and AGC



 $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right\}$  ,  $\left\{ \begin{array}{ccc} 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right\}$ Ε  $QQ$ 19 / 56

<span id="page-50-0"></span>Crash course on Droop and AGC

Answer is similar to the airplane: *local control shapes the aggregate so it* is more easily controlled.



Frequency response AGC(t)  $\longrightarrow \omega(t)$  is flat in region of interest

 $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right.$ B  $QQ$ 20 / 56

<span id="page-51-0"></span>Secondary Control Balancing Authority has a simple job

Control theorists in the audience:

what should the BA do?



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<span id="page-52-0"></span>Secondary Control Balancing Authority has a simple job

Control theorists in the audience:

what should the BA do?



Pure integral control is appropriate: set bandwidth near  $10^{-1}$  rad/sec.

## <span id="page-53-0"></span>Secondary Control Balancing Authority: Examples of AGC

AGC at PJM:



 $AGC(t) = RegA(t) + RegD(t)$ 

 $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right\}$  ,  $\left\{ \begin{array}{ccc} 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right\}$  $QQ$ 22 / 56

<span id="page-54-0"></span>Secondary Control Balancing Authority: Examples of AGC

#### Balancing Reserves at BPA:



Far more low frequency content – absence of r[ea](#page-53-0)l [ti](#page-55-0)[m](#page-53-0)[e](#page-59-0) ["](#page-55-0)e[n](#page-34-0)e[r](#page-60-0)[gy](#page-33-0)["](#page-59-0)[ma](#page-1-0)[rke](#page-142-1)t

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<span id="page-55-0"></span>Example of service from coal-fire power plants:



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<span id="page-56-0"></span>Example of service from coal-fire power plants:



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Data from [\[6\]](#page-139-2). Not a risk to stability, but *costly* [\[15\]](#page-141-0)

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<span id="page-57-0"></span>Where do they find Ancillary Services to provide needed actuation?

Many generalized storage solutions. If we are stuck with generators, then gas-combustion or hydro generation are best in terms of responsiveness.

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Also,

<span id="page-58-0"></span>Where do they find Ancillary Services to provide needed actuation?

Many generalized storage solutions. If we are stuck with generators, then gas-combustion or hydro generation are best in terms of responsiveness.

Also, compressed air, flywheels, molten salt, trains pulled up a hill, ...

[https://en.wikipedia.org/wiki/Grid\\_energy\\_storage](https://en.wikipedia.org/wiki/Grid_energy_storage)

#### <span id="page-59-0"></span>Where do they find Ancillary Services to provide needed actuation?

Many generalized storage solutions. If we are stuck with generators, then gas-combustion or hydro generation are best in terms of responsiveness.

Also, compressed air, flywheels, molten salt, trains pulled up a hill, ...

[https://en.wikipedia.org/wiki/Grid\\_energy\\_storage](https://en.wikipedia.org/wiki/Grid_energy_storage)



California believes the answer is ma[ssi](#page-58-0)[ve](#page-60-0) [b](#page-56-0)[a](#page-57-0)[t](#page-60-0)t[e](#page-59-0)[ri](#page-34-0)e[s](#page-60-0)

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## Virtual Energy Storage

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## Virtual Energy Storage





## Virtual Energy Storage

## <span id="page-63-0"></span>**Batteries**

Preferred in the Golden State

They are absolutely awesome, except costly and

## <span id="page-64-0"></span>**Batteries**

Preferred in the Golden State

They are absolutely awesome, except costly and

- Like pumped hydro, energy wasted with charge and discharge
- Lots of real-estate required, and lots of raw materials

(China has its eyes on Chile)

## <span id="page-65-0"></span>**Batteries**

Preferred in the Golden State

They are absolutely awesome, except costly and

- Like pumped hydro, energy wasted with charge and discharge
- Lots of real-estate required, and lots of raw materials

(China has its eyes on Chile)

• Eccentric charge/discharge rates:



Question: How can a fleet of batteries provide high-frequency ancillary service, such as PJM RegD?  $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right.$ 

<span id="page-66-0"></span>Some History

#### **• Schweppe's FAPER Concept**

#### Frequency adaptive, power-energy rescheduler

**US 4317049 A** 

#### **ABSTRACT**

A frequency adaptive, power-energy re-scheduler (FAPER) that includes a frequency transducer that notes frequency or frequency deviations of an electrical system and logic means which controls and re-schedules power flow to a load unit in part on the basis of the deviations in frequency from a nominal frequency and in part on the needs to the load unit as expressed by an external sensor signal obtained from the physical system affected by the load unit.



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<span id="page-67-0"></span>Some History

- **Schweppe's FAPER Concept**
- $\bullet$  Mathematical foundations: Malhamé et. al. in 80s [Mean-Field Model]

## <span id="page-68-0"></span>Demand Dispatch & Virtual Energy Storage Some History

- **Schweppe's FAPER Concept**
- Mathematical foundations: Malhamé et. al. in 80s [Mean-Field Model]
- Randomized control: Callaway, Hiskens, Mathieu, Kizilkale, Malham´e, Strbac, Almassalkhi, Hines Often system inversion to obtain linear MFM

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<span id="page-69-0"></span>Some History

- Mathematical foundations: Malhamé et. al. in 80s [Mean-Field Model]
- **A** Randomized control:

Callaway, Hiskens, Mathieu, Kizilkale, Malham´e, Strbac, Almassalkhi, Hines Often system inversion to obtain linear MFM

● Dozen papers by Meyn & Bušić since 2012 (see references)

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<span id="page-70-0"></span>Some History

• Industry now recognizes the value of randomization for distributed control

<span id="page-71-0"></span>Some History

#### • Industry now recognizes the value of randomization for distributed control

#### **Electrical load disconnect device with electronic control US 8328110 B2**

#### **ABSTRACT**

Electrical load spreading arrangements reduce peak power demand. An enclosure houses an electronic circuit board, which receives at a first input terminal a first thermostat control signal from a thermostat intended to control a first air conditioning unit and at a second input terminal a second thermostat control signal from a thermostat intended to control a second AC unit. A controller on the circuit board is programmed with instructions stored in a memory coupled to the controller causing the controller to monitor the first and second input terminals to determine the timing and duration of the thermostat control signals passed to the output terminals for activating or deactivating the



AC units such that overlapping operation of the AC units is reduced particularly during peak demand periods. A similar arrangement may be applied to a broader class of HVAC equipment, including water heaters, for example.

**IMAGES** (5)



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## <span id="page-72-0"></span>Demand Dispatch & Virtual Energy Storage Big Business

For more than thirty years:

- On Call<sup>a</sup>: Utility controls water heaters, residential pool pumps and other loads.
- **EDF** Sheds nuclear power load at night – electricity goes to heating Parisian water heaters

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<sup>&</sup>lt;sup>a</sup> Florida Power and Light, Florida's largest utility. [www.fpl.com/residential/energysaving/programs/oncall.shtml](www.fpl.com/residential/energysaving/programs/oncall.shtml )

## <span id="page-73-0"></span>Demand Dispatch & Virtual Energy Storage Big Business

For more than thirty years:

- On Call<sup>a</sup>: Utility controls water heaters, residential pool pumps and other loads.
- **EDF** Sheds nuclear power load at night – electricity goes to heating Parisian water heaters
- Similar programs with long history in New Zealand & UK

<sup>&</sup>lt;sup>a</sup> Florida Power and Light, Florida's largest utility. [www.fpl.com/residential/energysaving/programs/oncall.shtml](www.fpl.com/residential/energysaving/programs/oncall.shtml )

## <span id="page-74-0"></span>Demand Dispatch & Virtual Energy Storage

Potential Big Business



## <span id="page-75-0"></span>Capacity of Virtual Energy Storage



<span id="page-76-0"></span>HVAC flexibility to provide additional ancillary service

- Buildings consume 70% of electricity in the US
- Buildings have large thermal capacity

<span id="page-77-0"></span>HVAC flexibility to provide additional ancillary service

- Buildings consume 70% of electricity in the US
- Buildings have large thermal capacity
- Modern buildings have fast-responding equipment: VFDs (variable frequency drive)



<span id="page-78-0"></span>Tracking RegD at Pugh Hall

In one sentence: Ramp up and down power consumption, just 10%, to track regulation signal.

<span id="page-79-0"></span>Tracking RegD at Pugh Hall

In one sentence: Ramp up and down power consumption, just 10%, to track regulation signal.



ignore the measurement noise

How demand response from commercial buildings will provide the regulation ..., Allerton, 2012  $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right\}$  ,  $\left\{ \begin{array}{ccc} 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right\}$  $QQ$ 31 / 56

# <span id="page-80-0"></span>Pugh Hall @ UF

How much?



- . One AHU fan with 25 kW motor:  $> 3$  kW of regulation reserve
- $\triangleright$  Pugh Hall (40k sq ft, 3 AHUs):  $> 10$  kW

Indoor air quality is not affected

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# <span id="page-81-0"></span>Pugh Hall @ UF

How much?



- $\triangleright$  One AHU fan with 25 kW motor:  $> 3$  kW of regulation reserve
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 $\triangleright$  100 buildings:  $> 1$  MW

# <span id="page-82-0"></span>Pugh Hall @ UF

How much?



- $\triangleright$  One AHU fan with 25 kW motor:  $> 3$  kW of regulation reserve
- $\triangleright$  Pugh Hall (40k sq ft, 3 AHUs):  $> 10$  kW

Indoor air quality is not affected

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 $\triangleright$  100 buildings:  $> 1$  MW

just using 10% of the fans

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- Virtual energy storage (MWh)
- Virtual power (MW)

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- Virtual energy storage (MWh)
- Virtual power (MW)

#### Power Capacity

Average power consumption:  $P_{\text{avg}} = 30 \text{ MW}$  (without usage) Peak power:  $P_{\text{peak}} > 500$  MW

<span id="page-85-0"></span>

- Virtual energy storage (MWh)
- Virtual power (MW)

#### Power Capacity

Average power consumption:  $P_{\text{avg}} = 30 \text{ MW}$  (without usage) Peak power:  $P_{\text{peak}} > 500$  MW

**Answer:**  $P_+ = P_{\text{avg}}$  and  $P_- = P_{\text{peak}} - P_{\text{avg}}$ 

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- Virtual energy storage (MWh)
- Virtual power (MW)

### Energy Capacity

Suppose system is fully charged at time  $t = 0$ .  $T =$  time to discharge: All units off for  $0 \le t \le T$ 

<span id="page-87-0"></span>

- Virtual energy storage (MWh)
- Virtual power (MW)

### Energy Capacity

Suppose system is fully charged at time  $t = 0$ .  $T =$  time to discharge: All units off for  $0 \le t \le T$ 

**Answer:**  $E = T \times P_{\text{avg}}$ 

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#### Energy Capacity

Suppose system is fully charged at time  $t = 0$ .  $T =$  time to discharge: All units off for  $0 \le t \le T$ 

**Answer:**  $E = T \times P_{\text{avg}}$ 



∼ agrees with H. Hao et. al., Aggregate flexibility of thermostatically controlled loads, 2015 [\[7\]](#page-140-0)<br>← □ ▶ ← △ ← ← △ ← ← △ ← ← △ ← △ ← △ ← △ ← ← △  $\equiv$ 33 / 56

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<span id="page-89-0"></span>**Capacity** 120,000 residential water heaters

# **Capacity**  $P_+ = P_{\text{avg}} = 30$  MW  $P_-=P_{\text{peak}}-P_{\text{avg}}$  $E = T \times P_{\text{avg}}$

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<span id="page-90-0"></span>**Capacity** 120,000 residential water heaters

# **Capacity**  $P_+ = P_{\text{avg}} = 30$  MW  $P_-=P_{\text{peak}}-P_{\text{avg}}$  $E = T \times P_{\text{avg}}$

Typical:  $T = 4$  hours

 $\approx$  30 MW, 120 MWh battery system

#### <span id="page-91-0"></span>**Capacity**

- $P_{+} = P_{\text{avg}} = 30$  MW
- $P_-=P_{\text{peak}}-P_{\text{avg}}$
- $E = T \times P_{\text{avg}}$
- Typical:  $T = 4$  hours



#### World's largest lithium-ion storage battery

TOPICS: Aliso Canyon alternative energy CPUC energy lithium-ion batteries Los Angeles sdg&e  $\sim 100$  and  $\sim 10$ 

 $\approx$  30 MW, 120 MWh battery system

## How do we compare?

 $\mathbf{A} \equiv \mathbf{A} + \mathbf{A} \mathbf{B} + \mathbf{A} \mathbf{B} + \mathbf{A} \mathbf{B} + \mathbf{B} \mathbf{B}$ 

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#### <span id="page-92-0"></span>**Capacity**

- $P_{+} = P_{\text{avg}} = 30$  MW  $P_-=P_{\text{peak}}-P_{\text{avg}}$
- $E = T \times P_{\text{avg}}$
- Typical:  $T = 4$  hours
	- $\approx$  30 MW, 120 MWh battery system

#### How do we compare?



30 MW, 120 MWh battery system!

#### <span id="page-93-0"></span>**Capacity**

 $P_+ = P_{\text{avg}} = 30$  MW  $P_-=P_{\text{peak}}-P_{\text{ave}}$  $E = T \times P_{\text{avg}}$ 

Typical:  $T = 4$  hours

 $\approx$  30 MW, 120 MWh battery system

### 30 MW, 120 MWh battery system!



The Escondido system consists of 24 containers hiding nearly 20,000 modules that hold 20 batteries each ... 10% round-trip energy loss, cooling required, ...

World's largest in Feb 2017; update in Dec: Tesla system in Australia is now the lead a[t 12](#page-92-0)[9](#page-94-0) [M](#page-88-0)[W](#page-89-0)[h](#page-95-0)  $QQ$ 34 / 56

#### <span id="page-94-0"></span>**Capacity**

- $P_+ = P_{\text{avg}} = 30$  MW  $P_-=P_{\text{peak}}-P_{\text{avg}}$  $E = T \times P_{\text{avg}}$
- Typical:  $T = 4$  hours

### $\approx$  30 MW, 120 MWh battery system

### 30 MW, 120 MWh battery system!



The Escondido system consists of 24 containers hiding nearly 20,000 modules that hold 20 batteries each ... 10% round-trip energy loss, cooling required, ...

The population of California is 40 million, and the electricity doesn't just go into the hot t[ub](#page-93-0)[s](#page-95-0)

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#### <span id="page-95-0"></span>**Capacity**

- $P_+ = P_{\text{avg}} = 30$  MW  $P_-=P_{\text{peak}}-P_{\text{avg}}$  $E = T \times P_{\text{avg}}$
- Typical:  $T = 4$  hours
	- $\approx$  30 MW, 120 MWh battery system

### 30 MW, 120 MWh battery system!



The Escondido system consists of 24 containers hiding nearly 20,000 modules that hold 20 batteries each ... 10% round-trip energy loss, cooling required, ...

**Conjecture:** It would be far cheaper to give a free water heater (with interface/comm. har[d](#page-89-0)ware)to e[a](#page-96-0)ch [o](#page-142-0)f  $10^5$  ho[us](#page-94-0)[eh](#page-96-0)[ol](#page-88-0)d[s](#page-95-0) [i](#page-96-0)[n](#page-59-0) [S](#page-95-0)an [D](#page-109-0)[i](#page-110-0)[eg](#page-1-0)o  $\Omega$ 

## <span id="page-96-0"></span>Tracking with 100,000 Water Heaters

Power Limits – Regulation



Tracking results with 100,000 water heaters, and the behavior of a single water heater in three cases, distinguished by the reference signal [\[1\]](#page-139-0).

Theoretical power capacity is approx 8 MW (with no flow)

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## <span id="page-97-0"></span>Tracking with 100,000 Water Heaters

Energy Limits – Ramps and Contingencies



Distributed Control Design for Balancing the Grid Using Flexible Loads, Springer 2018

# <span id="page-98-0"></span>Tracking with 10,000 Swimming Pools

Regulation and Contingencies



Simulation using 10,000 swimming pools that consume on average 5MW

Range of services provided by the one million residential pools in California: contingency reserves and balancing can be supplied simultaneously [\[3,](#page-139-1) [1\]](#page-139-0).

From Yue Chen's thesis [\[3\]](#page-139-1) YC moves to NREL this week!  $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right\}$  ,  $\left\{ \begin{array}{ccc} 0 & 0 & 0 \\ 0 & 0 & 0 \end{array} \right\}$ 

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 $\left\{ \begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \end{array} \right.$ 

## <span id="page-99-0"></span>DER Flexibility Assessment & Valuation Ongoing GMLC project – PNNL/ORNL/UF

Virtual Battery-Based Characterization and Control of Flexible Building Loads Using VOLTTRON



<span id="page-100-0"></span>Intelligence at the Load distinguishes our work from others

 $\rightarrow$  [No time for details – wait until next Wednesday!](#page-108-0)

#### Step 1: Load-level Feedback Loops



<span id="page-101-0"></span>Intelligence at the Load distinguishes our work from others

 $\rightarrow$  [No time for details – wait until next Wednesday!](#page-108-0)

#### Step 1: Load-level Feedback Loops



<span id="page-102-0"></span>Intelligence at the Load distinguishes our work from others

 $\rightarrow$  [No time for details – wait until next Wednesday!](#page-108-0)

#### Step 1: Load-level Feedback Loops

**Basic Ingredients:** 1. Randomized decision rule design. Maps  $(X, \zeta)$  to a probability of on/off 2. Secondary control monitors QoS, on slower time-scale



<span id="page-103-0"></span>Intelligence at the Load distinguishes our work from others

 $\rightarrow$  [No time for details – wait until next Wednesday!](#page-108-0)

#### Step 1: Load-level Feedback Loops

**Basic Ingredients:** 1. Randomized decision rule design. Maps  $(X, \zeta)$  to a probability of on/off 2. Secondary control monitors QoS, on slower time-scale 3. Newest innovation: additional filtering of  $\zeta$ to invert mean-field dynamics *in a specific frequency range* 



<span id="page-104-0"></span>Intelligence at the Load

#### Step 2: Condition Grid Reference Signal



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<span id="page-105-0"></span>Intelligence at the Load

Step 2: Condition Grid Reference Signal



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<span id="page-106-0"></span>Assume BA has measurements of aggregate power consumption

Step 3: Actuator Feedback Loop Easily controllable by design

<span id="page-107-0"></span>Assume BA has measurements of aggregate power consumption

Step 3: Actuator Feedback Loop Easily controllable by design





 $\Omega$ 41 / 56
### <span id="page-108-0"></span>Control Architecture

Aggregate input-output dynamics



linearized dynamics from BA to power deviation

## <span id="page-109-0"></span>Control Architecture

Aggregate input-output dynamics



linearized dynamics from BA to power deviation

[Det](#page-108-0)[ail](#page-110-1)[s](#page-107-0) [i](#page-108-0)[n](#page-109-0) [l](#page-110-1)[e](#page-110-1)[c](#page-100-0)[t](#page-109-0)[u](#page-110-1)[re](#page-59-0)ne[xt](#page-1-0) [we](#page-142-0)ek

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<span id="page-110-1"></span><span id="page-110-0"></span>

### Questions and Conclusions

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# <span id="page-111-0"></span>Question of Time Scales

Question: Can a smart fridge provide synthetic droop?

### <span id="page-112-0"></span>Question of Time Scales

Question: Can a smart fridge provide synthetic droop?

• There is hope: They did a good job in the past!

## <span id="page-113-0"></span>Question of Time Scales

Question: Can a smart fridge provide synthetic droop?

- There is hope: They did a good job in the past!
- Other local services may also be feasible and valuable

**Electrical load disconnect device with electronic control US 8328110 B2**

#### **ABSTRACT**

Electrical load spreading arrangements reduce peak power demand. An enclosure houses an electronic circuit board, which receives at a first input terminal a first thermostat control signal from a thermostat intended to control a first air conditioning unit and at a second input terminal a second thermostat control signal from a thermostat intended to control a second AC unit. A controller on the circuit board is programmed with instructions stored in a memory coupled to the controller causing the controller to monitor the first and second input terminals to determine the timing and duration of the thermostat control signals passed to the output terminals for activating or deactivating the



AC units such that overlapping operation of the AC units is reduced particularly during peak demand periods. A similar arrangement may be applied to a broader class of HVAC equipment, including water heaters, for example.



### <span id="page-114-0"></span>What if we lose  $\omega$ ?

One of the side-effects of replacing spinning machines with power electronics

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#### <span id="page-115-0"></span>What if we lose  $\omega$ ?

One of the side-effects of replacing spinning machines with power electronics

• Synthetic intertia  $-$  just to send a control signal?

## <span id="page-116-0"></span>What if we lose  $\omega$ ?

One of the side-effects of replacing spinning machines with power electronics

- Synthetic intertia just to send a control signal?
- Voltage?
- Alternate approaches to consensus? [\[25,](#page-142-1) [24\]](#page-142-2)



 $\mathcal{A} \cap \mathcal{B} \rightarrow \mathcal{A} \supseteq \mathcal{B} \rightarrow \mathcal{A} \supseteq \mathcal{B}$ 

a miller

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### <span id="page-117-0"></span>Question: Estimation

- Estimating the state for the MFM is not realistic in general [\[19\]](#page-141-0)
- Estimating the *baseline* is a philosophical question

### <span id="page-118-0"></span>Question: Estimation

- Estimating the *state* for the MFM is not realistic in general [\[19\]](#page-141-0)
- **•** Estimating the *baseline* is a philosophical question
- How do we define and estimate the State of Charge?

#### <span id="page-119-0"></span>Question: Estimation

- Estimating the *state* for the MFM is not realistic in general [\[19\]](#page-141-0)
- **•** Estimating the *baseline* is a philosophical question
- $\bullet$  How do we define and estimate the State of Charge?



For WHs: ∼function of average water temperature

### <span id="page-120-0"></span>Question: Impact on Consumers

- What is the cost to consumers? Any additional cycling or energy cost?
- A better science for enforcing QoS/cost constraints

... More on this next week

[Conclusions](#page-121-0) [Value of Performance](#page-121-0)

<span id="page-121-0"></span>

Regulation service from generators is not perfect

[Frequency Regulation Basics and Trends](http://tinyurl.com/KirbyBasics04) — Brendan J. Kirby, December 2004

[Conclusions](#page-122-0) [Value of Performance](#page-122-0)

<span id="page-122-0"></span>

The grid today is reliable<sup>∗</sup> , despite the poor services offered by generators Questions remain:

- What is the cost of poor tracking?
- How do we deal with dynamics/uncertainty in capacity of virtual storage from loads?

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#### <span id="page-123-0"></span>Question: Control Architecture Smart Fridge / Dumb Grid?

Local intelligence at each load  $\implies$  ensemble looks like a giant battery.



#### <span id="page-124-0"></span>Question: Control Architecture Smart Fridge / Dumb Grid?

Local intelligence at each load  $\implies$  ensemble looks like a giant battery.

Open-loop tracking with 40,000 heterogeneous TCLs:



Demand dispatch with heterogeneous intelligent loads, HICSS [20](#page-123-0)[17](#page-125-0)  $\rightarrow \rightarrow \rightarrow \rightarrow \rightarrow \rightarrow$  $\Omega$ 48 / 56

#### <span id="page-125-0"></span>Question: Control Architecture Smart Fridge / Dumb Grid?

Local intelligence at each load  $\implies$  ensemble looks like a giant battery.

• Does one-way communication suffice?



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<span id="page-126-0"></span>Rationality  $\implies$  risk-aware

Since Schweppe, there has been a passion for competitive equilibrium analysis, with power treated as the commodity of interest.



<span id="page-127-0"></span>Since Schweppe, there has been a passion for competitive equilibrium analysis, with power treated as the commodity of interest.

Trouble with current thinking:

Long-term risk. The marginal-cost framework does not provide adequate incentives for investment  $-$  this was recognized by EDF many decades ago.

<span id="page-128-0"></span>Since Schweppe, there has been a passion for competitive equilibrium analysis, with power treated as the commodity of interest.

Trouble with current thinking:

Long-term risk. The marginal-cost framework does not provide adequate incentives for investment  $-$  this was recognized by EDF many decades ago.

<span id="page-129-0"></span>Since Schweppe, there has been a passion for competitive equilibrium analysis, with power treated as the commodity of interest.

Trouble with current thinking:

Long-term risk. The marginal-cost framework does not provide adequate incentives for investment  $-$  this was recognized by EDF many decades ago.

- Short term risk faced by grid operator:
	- Will services be available when needed?
	- Quality sufficient?

<span id="page-130-0"></span>Since Schweppe, there has been a passion for competitive equilibrium analysis, with power treated as the commodity of interest.

Trouble with current thinking:

Long-term risk. The marginal-cost framework does not provide adequate incentives for investment  $-$  this was recognized by EDF many decades ago.

- Short term risk faced by grid operator:
	- Will services be available when needed?
	- Quality sufficient?
- What do consumers want?

<span id="page-131-0"></span>Since Schweppe, there has been a passion for competitive equilibrium analysis, with power treated as the commodity of interest.

Trouble with current thinking:

Long-term risk. The marginal-cost framework does not provide adequate incentives for investment  $-$  this was recognized by EDF many decades ago.

- Short term risk faced by grid operator:
	- Will services be available when needed?
	- Quality sufficient?
- What do consumers want? Risk comes in many flavors:
	- Is my power available?

<span id="page-132-0"></span>Since Schweppe, there has been a passion for competitive equilibrium analysis, with power treated as the commodity of interest.

Trouble with current thinking:

Long-term risk. The marginal-cost framework does not provide adequate incentives for investment  $-$  this was recognized by EDF many decades ago.

- Short term risk faced by grid operator:
	- Will services be available when needed?
	- Quality sufficient?
- What do consumers want? Risk comes in many flavors:
	- Is my power available?
	- Is my bill predictable?

<span id="page-133-0"></span>What do consumers want?

Rational agent in Berkeley wants a hot shower... (maybe with a nudge)

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<span id="page-134-0"></span>What do consumers want?

#### Rational agent in Berkeley wants a hot shower... (maybe with a nudge)



HOT-WATER THERMOSTAT HYSTERESIS ANALYSIS IBUILDERAT

Typical water heater trajectories  $\Theta(t)$ : Temperature  $G(t)$ : Power consumption

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<span id="page-135-0"></span>What do consumers want?

#### Rational agent in Berkeley wants a hot shower... (maybe with a nudge)



HOT-WATER THERMOSTAT HYSTERESIS ANALYSIS IBUILDERAT

Typical water heater trajectories  $\Theta(t)$ : Temperature  $G(t)$ : Power consumption

Not-so rational agent:  $m$ 

$$
\max_{G} \int_0^T \Bigl( \mathcal{U}(G(t)) - p(t)G(t) \Bigr) dt
$$

Big question: Science for long-term contracts that ensures

- Long-term incentives
- Appropriate risk allocation on every time-scale

<span id="page-136-0"></span>What do consumers want?

#### Rational agent in Berkeley wants a hot shower... (maybe with a nudge)



HOT-WATER THERMOSTAT HYSTERESIS ANALYSIS IBUILDERAT

Typical water heater trajectories  $\Theta(t)$ : Temperature  $G(t)$ : Power consumption

G  $\int_0^T$  $\boldsymbol{0}$  $\Bigl(\mathcal{U}(G(t)) - p(t) G(t)\Bigr) dt$ 

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Big question: Science for long-term contracts that ensures

- Long-term incentives
- Appropriate risk allocation on every time-scale
- Requires cost/value calculations for virtual energy storage

<span id="page-137-0"></span>

## Thank You

<span id="page-138-0"></span>Pre-publication version for on-line viewing. Monograph available for purchase at your favorite retailer More information available at http://www.cambridge.org/us/catalogue/catalogue.asp?isbn=9780521884419

#### [Control Techniques](http://www.meyn.ece.ufl.edu/archive/spm_files/CTCN/CTCN.html) FOR Complex Networks



Sean Meyn

**CAMBRIDGE** 

Markov Chains and [Stochastic Stability](http://www.meyn.ece.ufl.edu/archive/spm_files/book.html)

August 2008 Pre-publication version for on-line viewing. Monograph to appear Februrary 2009



S. P. Meyn and R. L. Tweedie

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