# <span id="page-0-0"></span>Formal backdoor detection games and deceptive alignment

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#### Backdoor defense, learnability and obfuscation

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#### **A** bstract

We introduce a formal notion of defendability against backdoors using a game between an attacker and a defender. In this game, the attacker modifies a function to behave differently on a particular input known as the "trigger", while behaving the same almost everywhere else. The defender then attempts to detect the trigger at evaluation time. If the defender succeeds with high enough probability, then the function class is said to be defendable. The key constraint on the attacker that makes defense possible is that the attacker's strategy must work for a randomly-chosen trigger.

Our definition is simple and does not explicitly mention learning, yet we demonstrate that it is closely connected to learnability. In the computationally unbounded setting, we use a voting algorithm of Hanneke et al. [2022] to show that defendability is essentially determined by the VC dimension of the function class, in much the same way as PAC learnability. In the computationally bounded setting, we use a similar argument to show that efficient PAC learnability implies efficient defendability, but not conversely. On the other hand, we use indistinguishability obfuscation to show that the class of polynomial size circuits is not efficiently defendable. Finally, we present polynomial size decision trees as a natural example for which defense is strictly easier than learning. Thus, we identify efficient defendability as a notable intermediate concept in between efficient learnability and obfuscation.

<sup>\*</sup>Work done while at the Alignment Research Center prior to April 2024.

# Deceptive alignment (a.k.a. "scheming")



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Ordinary and backdoored models behave almost the same, except when a secret "trigger" is present.

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#### Planting Undetectable Backdoors in Machine Learning Models



#### Abstract

Given the computational cost and technical expertise required to train machine learning models, users may delegate the task of learning to a service provider. Delegation of learning has clear benefits, and at the same time raises serious concerns of trust. This work studies possible abuses of power by untrusted learners.

We show how a malicious learner can plant an *undetectable backdoor* into a classifier. On the surface, such a backdoored classifier behaves normally, but in reality, the learner maintains a mechanism for changing the classification of any input, with only a slight perturbation. Importantly, without the appropriate "backdoor key," the mechanism is hidden and cannot be detected by any computationally-bounded observer. We demonstrate two frameworks for planting undetectable backdoors, with incomparable guarantees.

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Goldwasser, Kim, Vaikuntanathan, Zamir: no.

- Black-box (query access): defender cannot find an input on which the models differ (attack works for any learning algorithm).
- White-box (access to weights): defender cannot distinguish models (attack works for Random Fourier Features learning algorithm).

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Principles for our formal backdoor detection game:

- **a** White-box
- **b** Dynamic (i.e., runtime)
- **c** Worst-case assumptions ...

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- Worst-case assumptions ...
- $\bullet$  ... except the trigger is chosen randomly

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The defender wins with confidence  $\rightarrow 1 \iff \varepsilon = o\left(\frac{1}{\sqrt{C}}\right)$  $\frac{1}{\mathsf{VC}(\mathcal{F})}\bigg).$ 

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$$
.

## Proof sketch.

 $\implies$ : Same idea as whiteboard example.

 $\leftarrow$  : Defender "distills" given function to remove backdoor (and takes a majority vote [1]).

[1] S. Hanneke, A. Karbasi, M. Mahmoody, I. Mehalel, and S. Moran. On optimal learning under targeted data poisoning. NeurIPS, 2022.

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## Definition

 ${\cal F}$  is *efficiently defendable* **if** whenever  $\varepsilon < 1/\text{poly}(n, \frac{1}{\delta})$ , the defender can win with probability  $1-\delta$  using a poly  $(n,\frac{1}{\delta})$  $\frac{1}{\delta}$ )-time detection strategy. ( $n \approx$  number of bits needed to specify a point from X / a function from F)

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## **Corollary**

F is efficiently PAC learnable  $\implies$  F is efficiently defendable.

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### Proof sketch.

Use a secret key to "puncture" a pseudorandom function at a particular point, and use program obfuscation (iO) to hide the puncturing.

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BUT maybe we can spot the "secret key" by observing training?

For the CS theorists:

Question

Is the class of polynomial size Boolean formulas efficiently defendable?

For the alignment researchers:

## Question

How can we leverage information about the training process to dynamically detect backdoors and/or deceptive alignment?

### <span id="page-26-0"></span>Paper: <https://arxiv.org/abs/2409.03077>

ARC blog: <https://www.alignment.org/blog/>

