

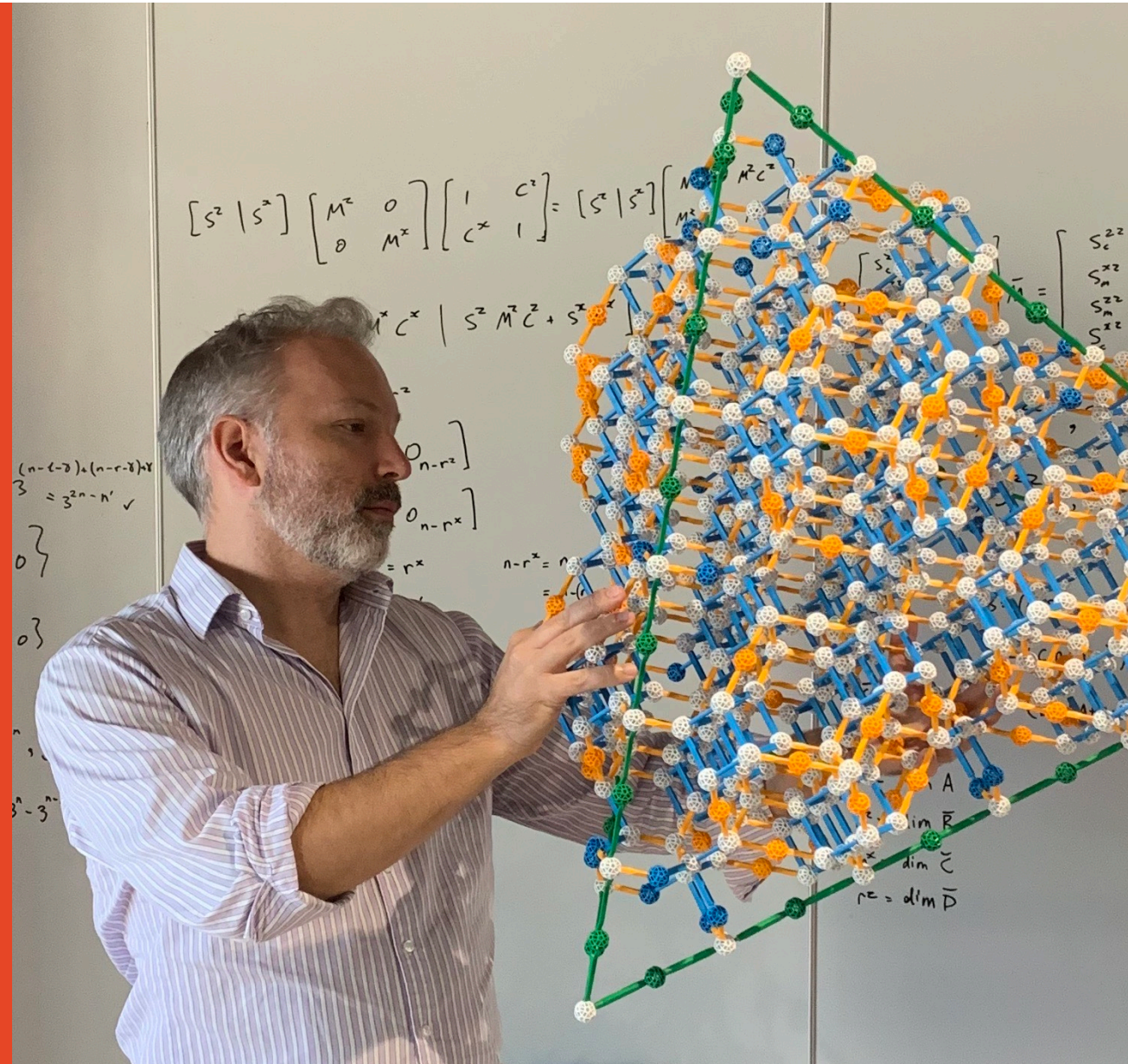
# Dawn in the age of quantum fault tolerance

Professor Stephen Bartlett

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**EQUS**  
Australian Research Council  
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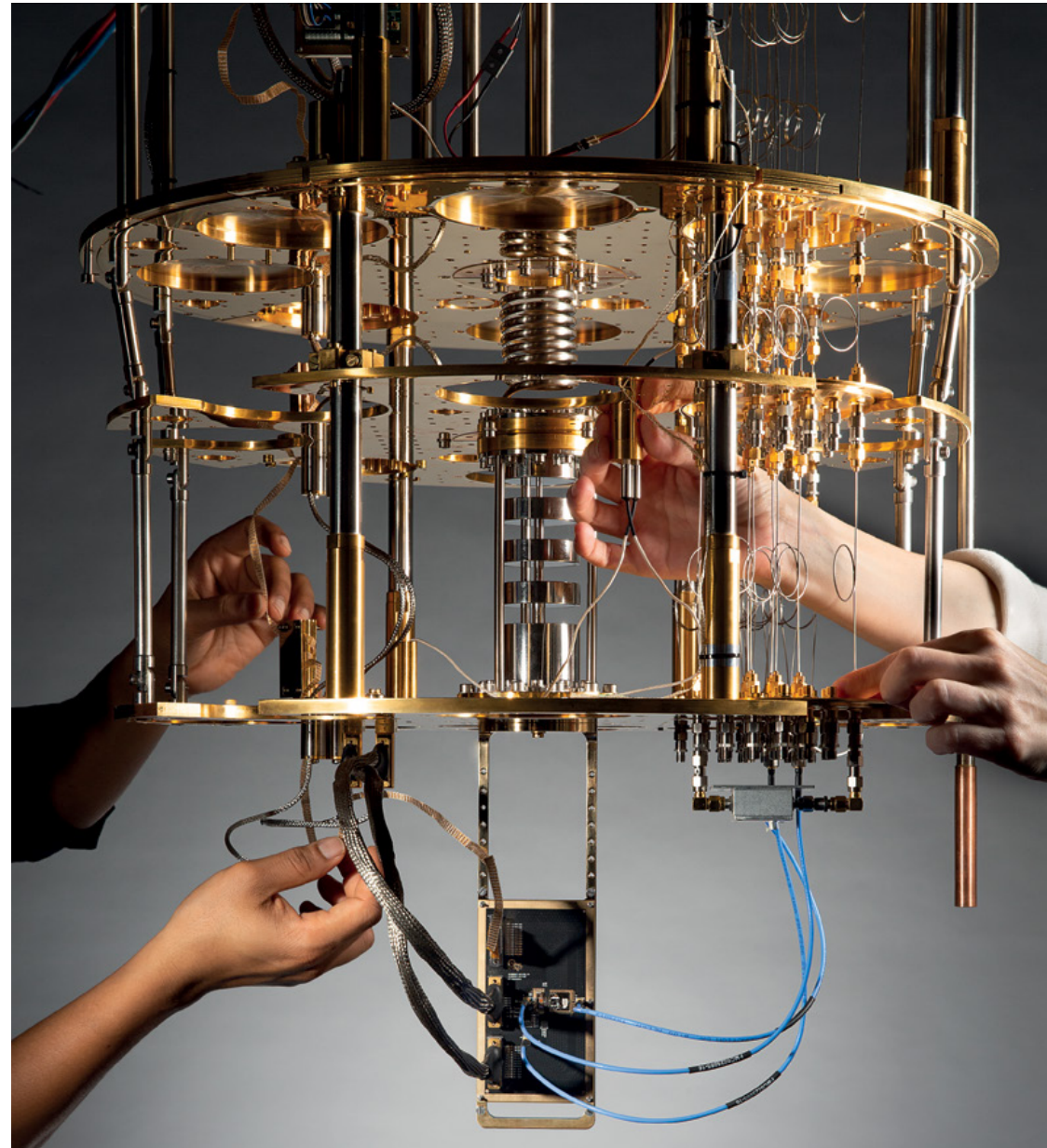


# QEC and fault tolerance

## An overview

## ‘Practical’ quantum computing

- Most of the interesting quantum algorithms we want to execute require large quantum circuits & many qubits
- Current qubit technologies fail too frequently (error rates a fraction of a per cent) to execute interesting instances
- Hardware is improving, but is unlikely to close the gap
- *Fault tolerant quantum computing is a catch-all term, describing architectures to perform large quantum computations using faulty parts*



## Quantum computing fault-tolerantly

### Physical qubits

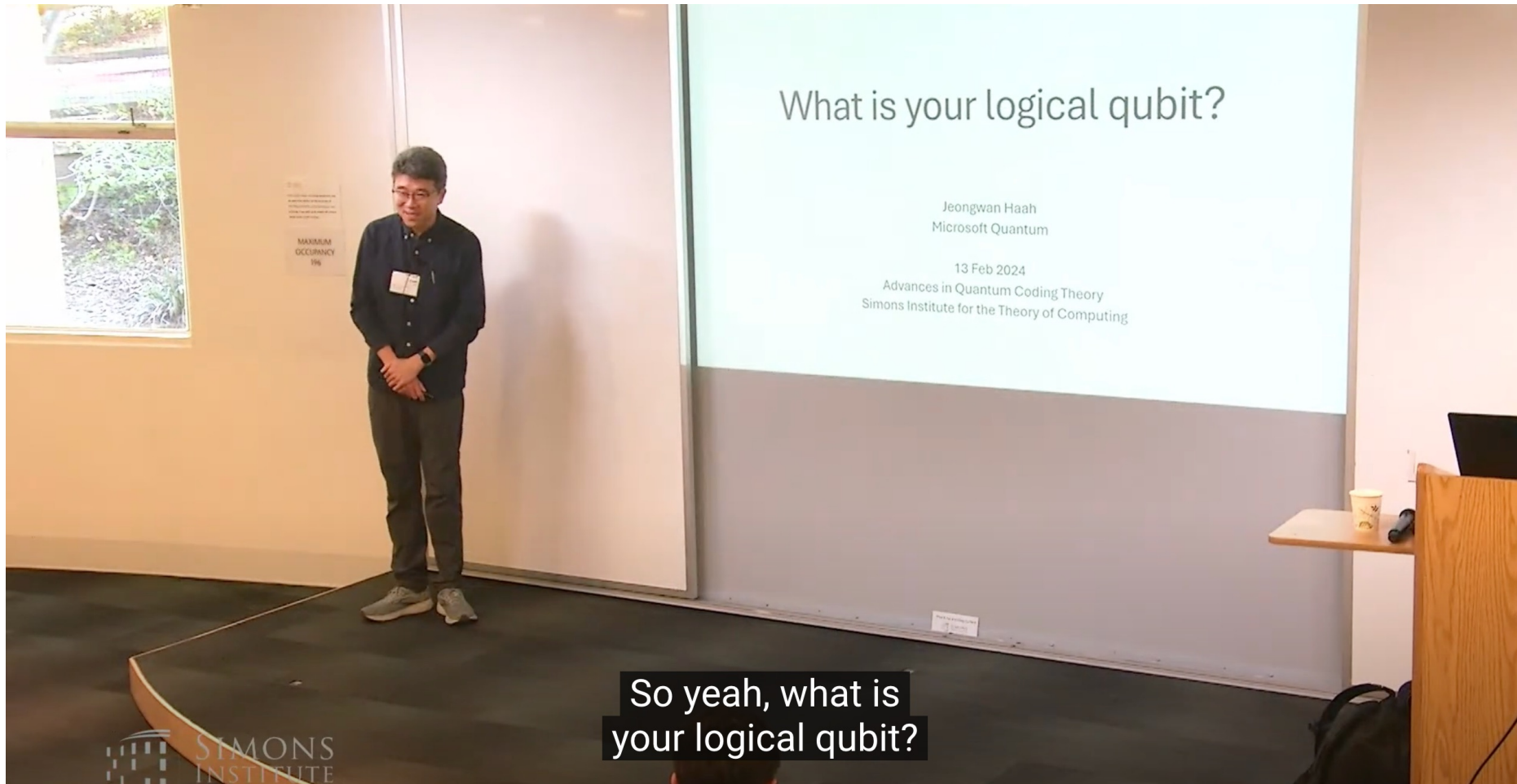
Noisy: failure rates a fraction of a percent per clock cycle

QEC code



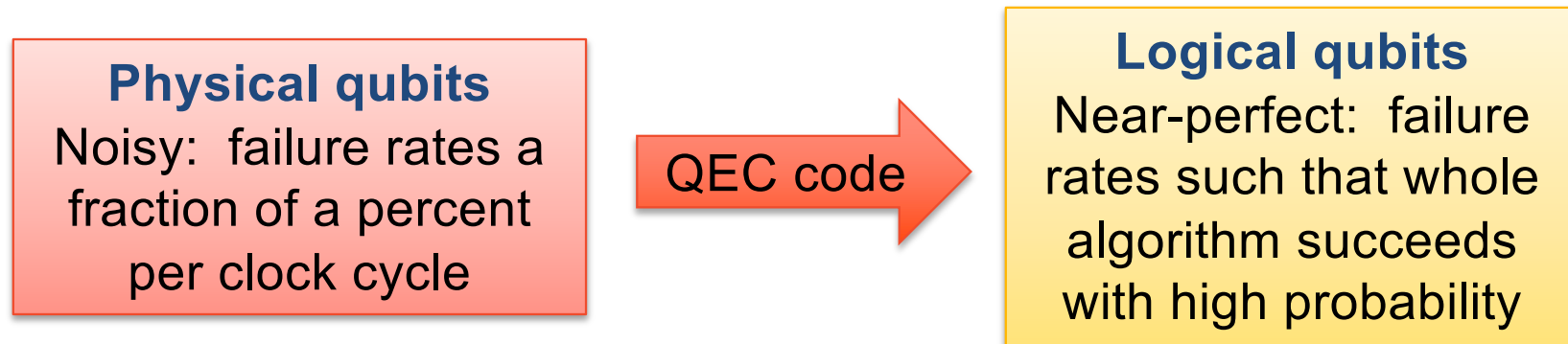
### Logical qubits

Near-perfect: failure rates such that whole algorithm succeeds with high probability



[https://www.youtube.com/watch?v=l4smz\\_J8f1E](https://www.youtube.com/watch?v=l4smz_J8f1E)

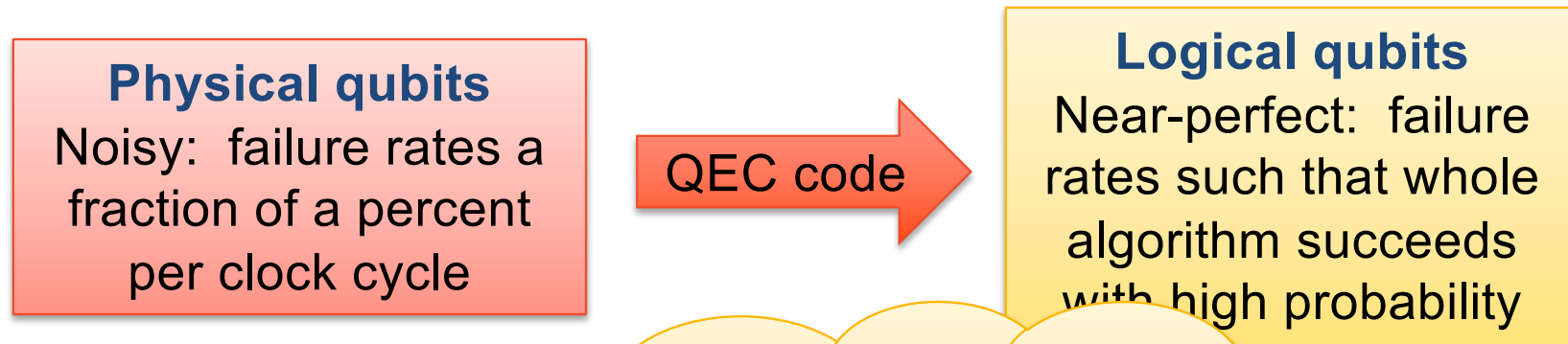
## Quantum computing fault-tolerantly



- Is this even possible? Requires physical error rates below a **threshold**.
  - Depends on code, the architecture, and the physical nature of the errors
  - Logic gates including QEC must be performed **fault-tolerantly**, to keep errors correctable (don't allow errors to spread or multiply)
  - Fault tolerance is a property of the **whole circuit**, not just a logical qubit or logical gate

D. Gottesman, Quantum fault-tolerance in small experiments,  
arXiv:1610.03507

# Quantum computing fault-tolerantly



- Is this even possible?
  - Depends on the error rate of the errors
  - Logic gates must be performed fault-tolerantly, to keep errors from multiplying)
  - Fault tolerance is not just a logical qubit

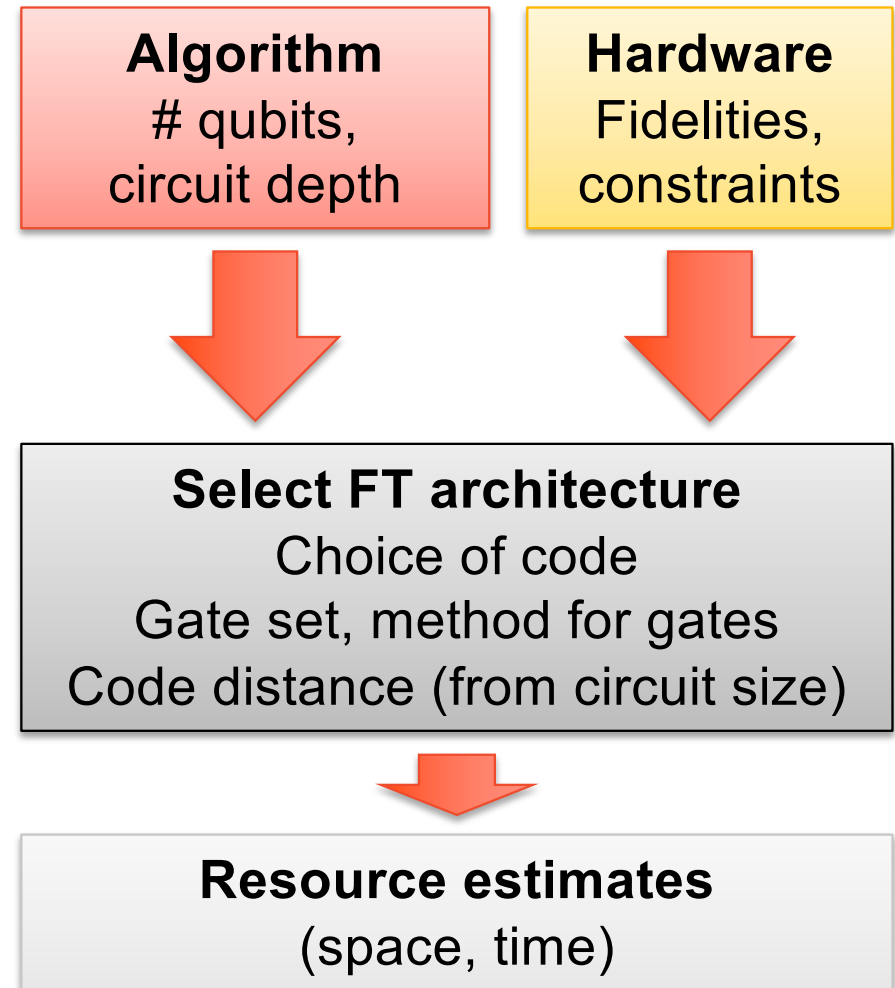
## Observation (Jeongwan's):

Characterising the 'fault tolerance' of a logical qubit or gate requires care

J. Gottesman, Quantum fault-tolerance in small experiments, arXiv:1610.03507

## Fault tolerance, overheads, and resources

- Step back and take a 'whole circuit' approach
- Threshold theorem states that an algorithm can be executed on (not too) noisy hardware with only a 'small' overhead
- **But what happens in practice?**

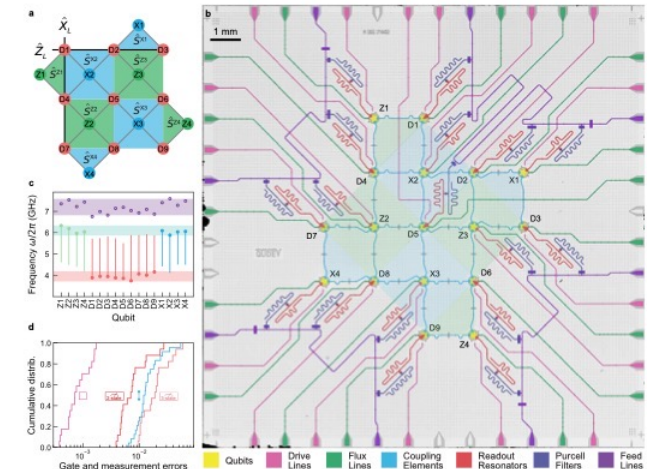
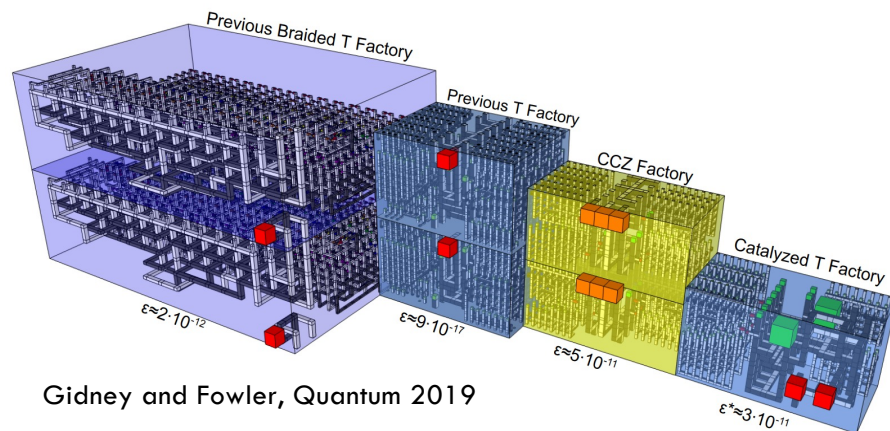




# Fault tolerant architectures

## Tolerance to errors: quantum error correcting codes

- 'Topological' stabilizer codes in a planar layout ('on a chip')
- Nearest-neighbour couplings (no long range couplings required)
- High error thresholds (0.1% - 1% error rates can be tolerated)
- Several hardware platforms now comfortably below threshold
- Bosonic codes offer competitive, even better performance



Krinner et al, Nature 2022

## But at a cost: resource overheads

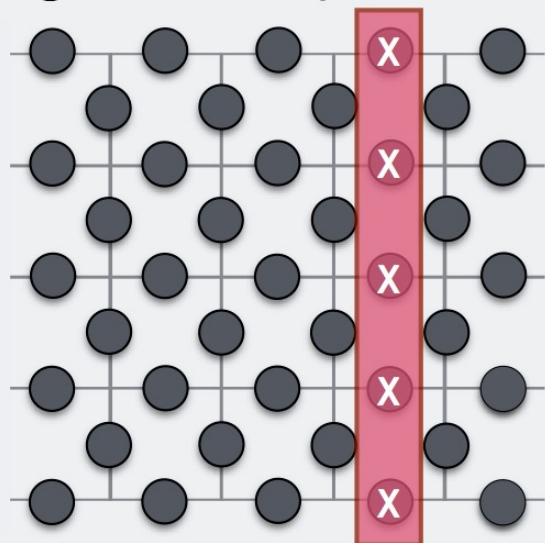
- Many candidate codes require thousands, millions of physical qubits to encode a single logical qubit
- Measurements in QEC repeated many times to be reliable
- Resource overheads for logic gates are also astronomical
- e.g. 20 million noisy qubits and 8 hours to run a complex q. algorithm

## Main messages:

- quantum error correction is becoming possible right now
- using current approaches at scale will be complex and costly

## Logic gates

- logical **X** operator:



- Logical qubits are spread across many physical qubits in a code
- Performing logic gates requires acting on many physical qubits simultaneously
- **Transversal logic gates:**
  - Apply independent physical gates
  - Naturally fault-tolerant
  - Constant depth (but still require FT QEC)
- **General logic gates:**
  - Complex constructions to make FT
  - e.g. Magic state distillation & injection
  - Significant time overheads

**Stabilizer codes:**  
A common class of quantum codes



Many popular codes have only **Clifford gates** as transversal



Circuits with only Clifford gates are not **universal** for QC

# Dogma

## Clifford logic gates

Easy  
Fault-tolerant  
“Classical”

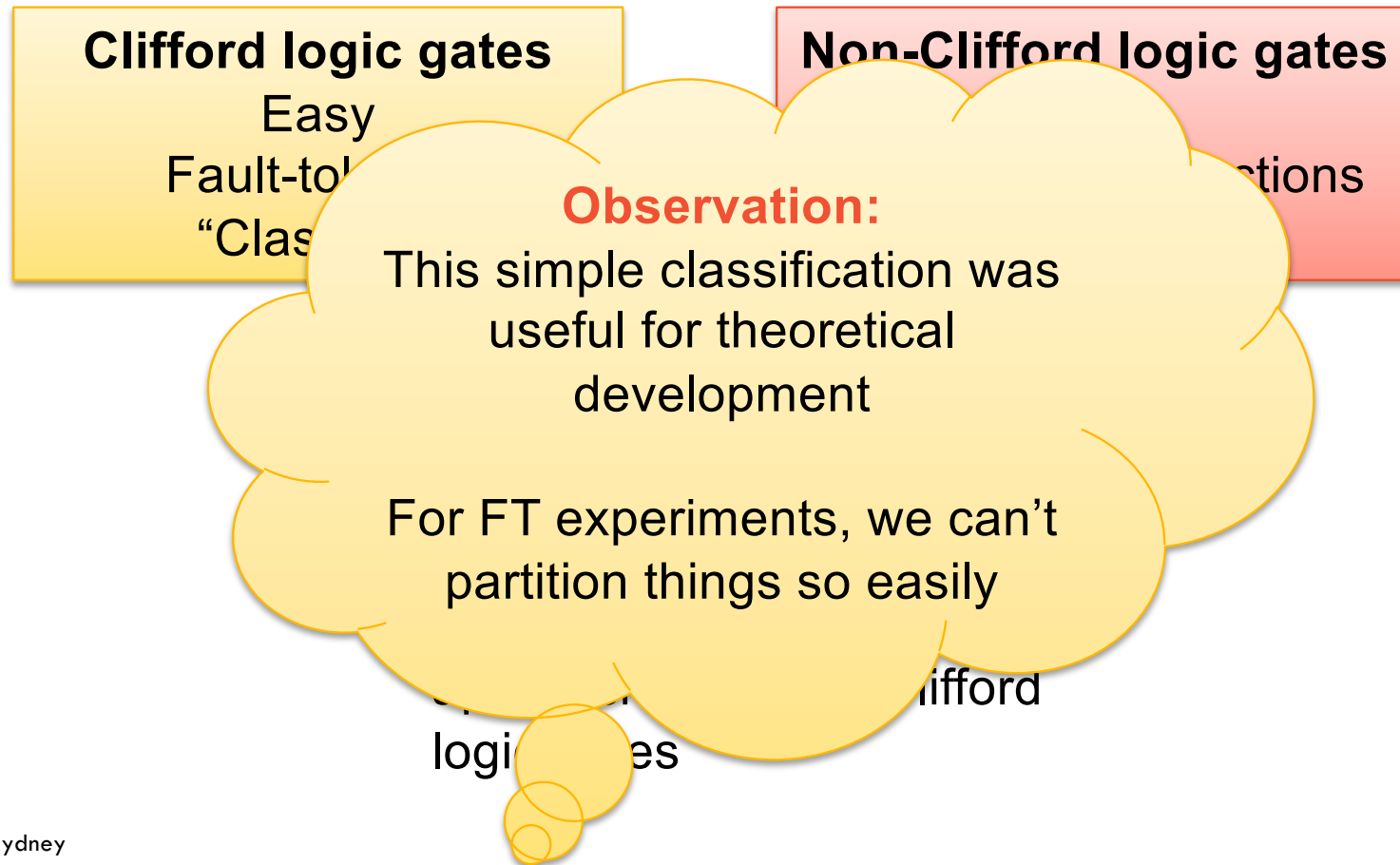
## Non-Clifford logic gates

Hard  
Costly FT constructions  
“Quantum”

### Designing FTQC:

- use classical resources to simulate Clifford logic gates
- focus on low-overhead approaches to non-Clifford logic gates

# Dogma

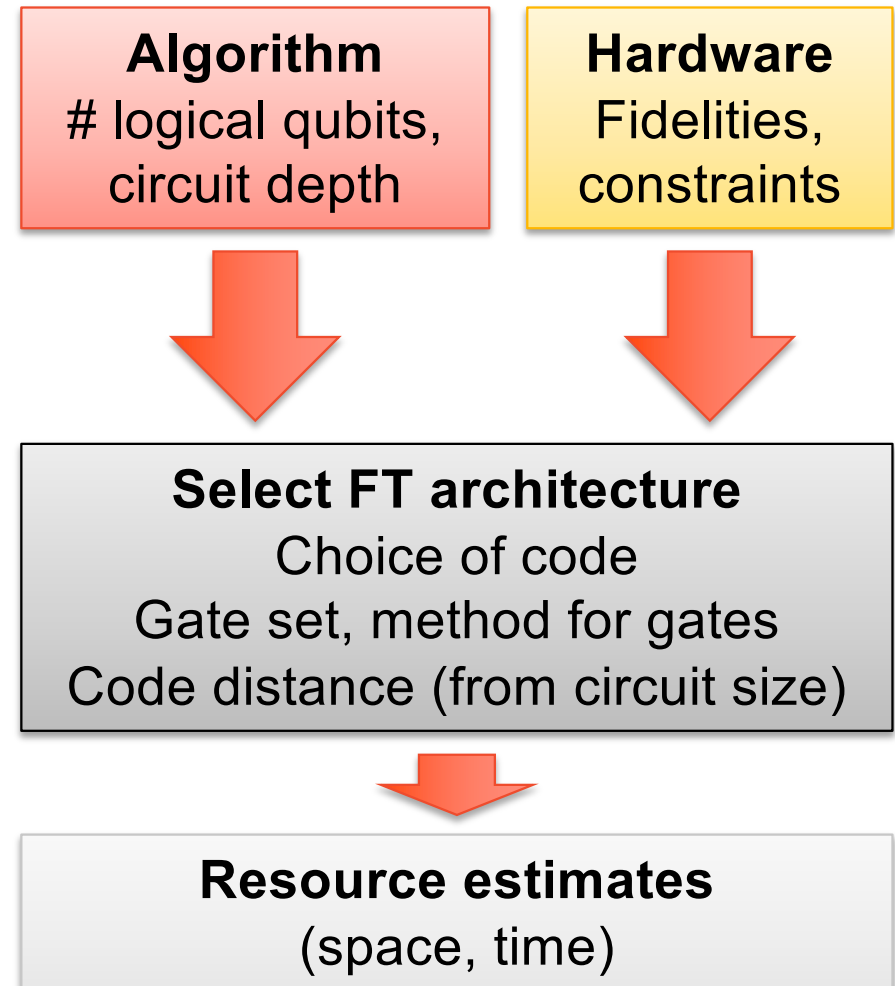


# Fault tolerant architectures

Scratching the surface of the  
surface code

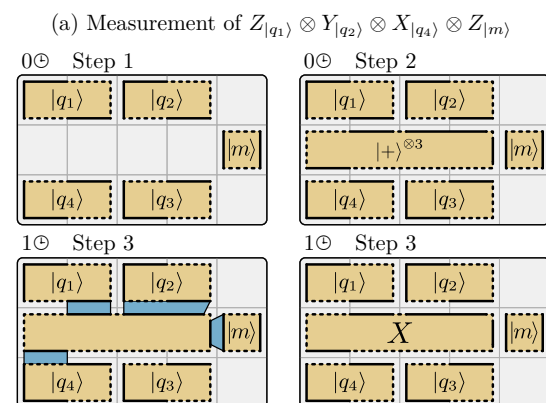
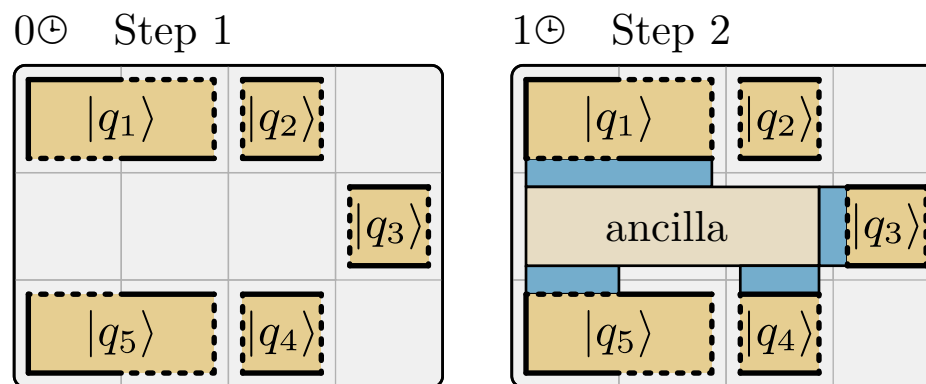
## Fault tolerance, overheads, and resources

- Different FTQC approaches lead to overheads that vary by many orders of magnitude
- Common choice of code is the **surface code**, due to high threshold and local 2D layout
- Given the surface code, an approach to gates that offers the *current* lowest overheads is **lattice surgery**



# Intro to FTQC with surface codes and lattice surgery

- State of the art: Litinski 2019 ('A game of surface codes') with some mods
- Convert logical quantum circuit into 'Pauli-based computation'
  - Many nontrivial aspects to this step
- Lattice surgery: a method to fault-tolerantly perform multi-logical-qubit Pauli measurements to perform gates
- Options for space vs time tradeoffs
- Data blocks and distillation blocks
  - Lots of assumptions and choices of distillation scheme, and overheads
- Provides a direct way to estimate space and time overheads



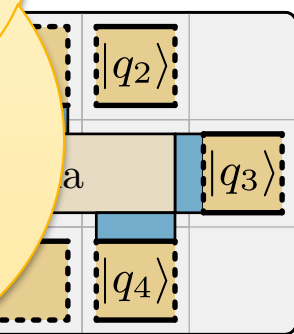
# Intro to FTQC with surface codes

- State of the art
- Convert logical based comp
  - **Many**
- Lattice surg
  - tolerantly per
  - Pauli measure
- Options for s
- Data blocks a
  - **Lots of assum**
  - **distillation scheme**
- Provides a direct way to es
  - and time overheads

**Observation:**  
 Surface code is particularly costly.  
 Lots of opportunity for disruption  
 More exotic topological codes,  
 qLDPC codes  
 More work to be done on codes  
 with non-Clifford transversal gates

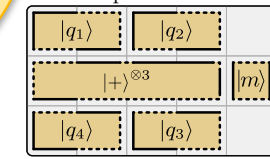
some mods

p 2

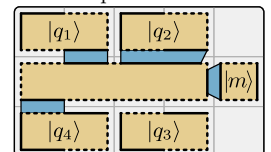


$$\otimes Y_{|q_2\rangle} \otimes X_{|q_4\rangle} \otimes Z_{|m\rangle}$$

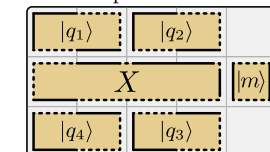
0⊗ Step 2



1⊗ Step 3



1⊗ Step 3



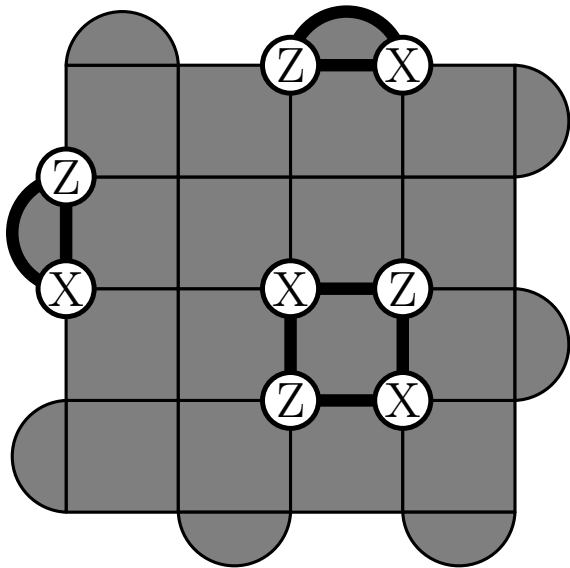


# Lowering the overheads

## FTQC with LDPC, ASAP

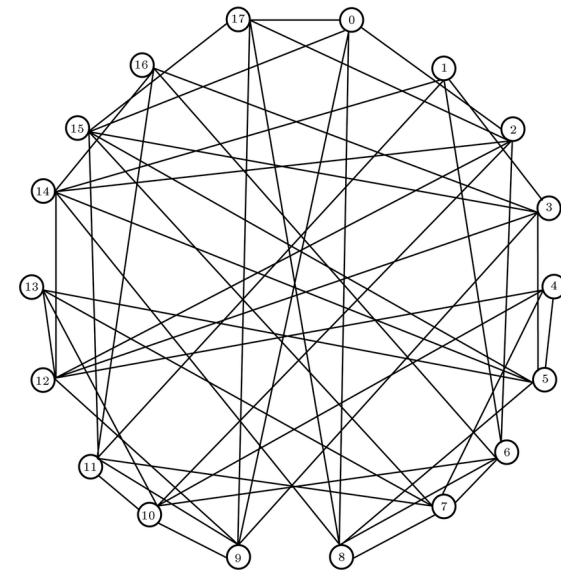
# Topological codes vs qLDPC codes

Surface code has local check operators



More protection with larger systems  
Encodes **one** logical qubit no matter  
how big

qLDPC codes remove the locality constraint



More protection with larger systems  
Encodes **many** logical qubits,  
growing with size

## Recent breakthrough: good codes!

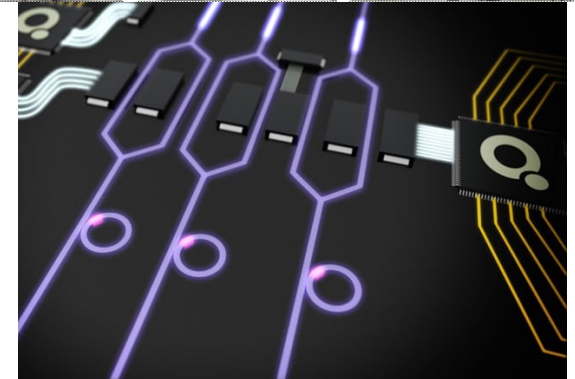
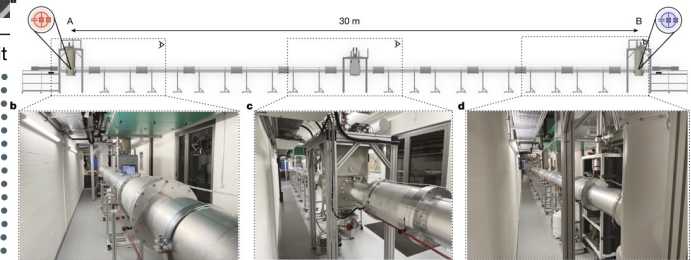
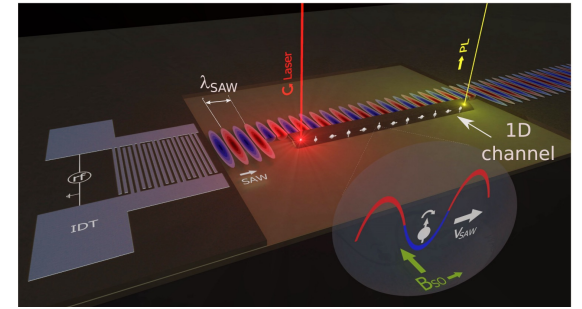
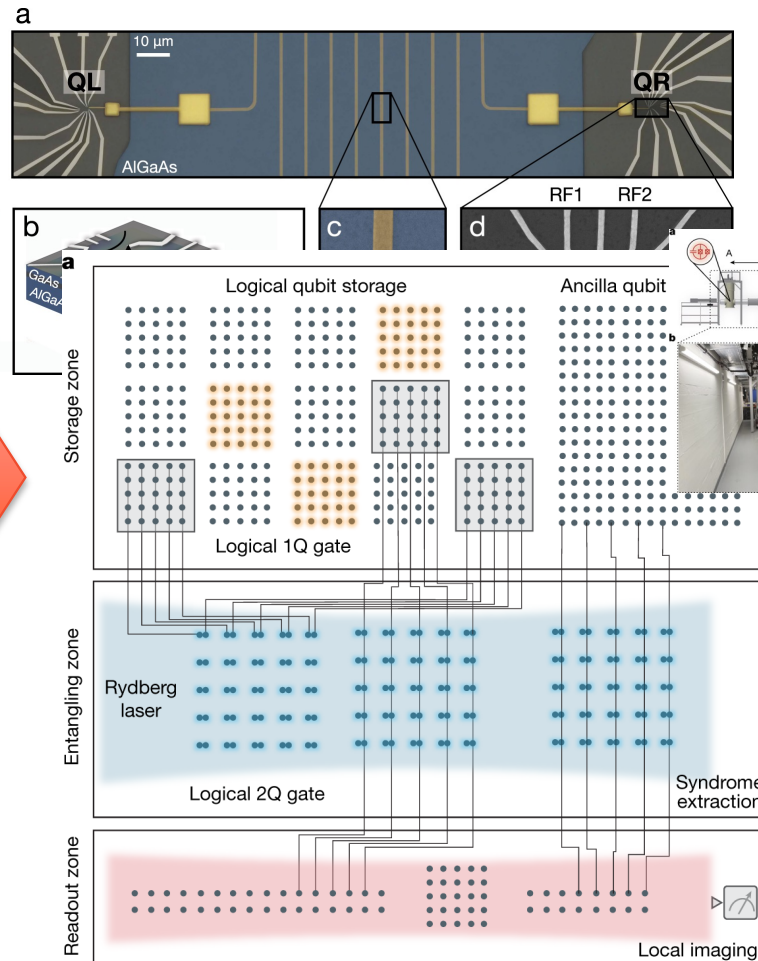
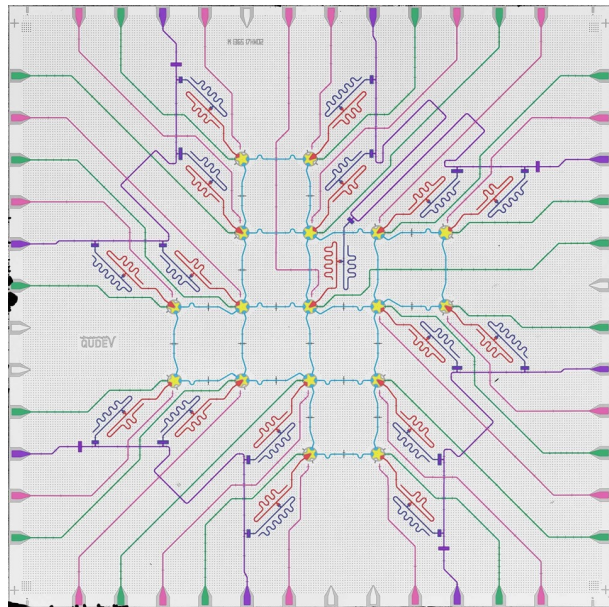
$k$	$d$	Code
2	$\sqrt{n}$	Kitaev toric
2	$\sqrt{n\sqrt{\log n}}$	Freedman-Meyer-Luo
$\Theta(n)$	$\sqrt{n}$	hypergraph product
$\sqrt{n}/\log n$	$\sqrt{n} \log n$	high-dimensional expander (HDX)
$\sqrt{n}$	$\sqrt{n} \log^c n$	tensor-product HDX
$n^{3/5}/\text{polylog}(n)$	$n^{3/5}/\text{polylog}(n)$	fiber-bundle
$\log n$	$n/\log n$	lifted-product (LP)
$\Theta(n)$	$\Theta(n)$	expander LP
$\Theta(n)$	$\Theta(n)$	quantum Tanner
$\Theta(n)$	$\Theta(n)$	Dinur-Hsieh-Lin-Vidick

} Yay!

Table 1: Notable QLDPC codes;  $c$  is a positive integer.

From EC Zoo <https://errorcorrectionzoo.org/c/qldpc>

# Don't we need geometrically local gates?



## But...

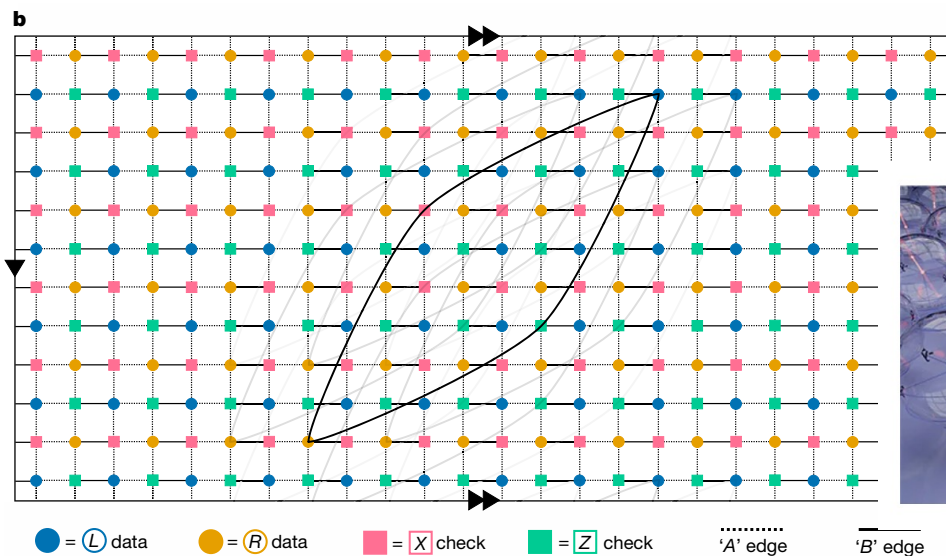
- Is there a low-overhead architecture based on a high-rate qLDPC code?

D. Gottesman, Fault-Tolerant Quantum Computation with Constant Overhead, arXiv:1310.2984

- The ingredients are there:
  - codes that satisfy Gottesman's criteria
  - reasonably high thresholds and fast decoders
- But focus has been on asymptotics. What about in practice?

# qLDPC codes and FTQC

- Recent proposals look to use qLDPC codes in current and future hardware to reduce overheads
- What are the actual gains in the relevant regimes?
- What long-range connectivity is needed, or most useful?



The University of Sydney

## Article

# High-threshold and low-overhead fault-tolerant quantum memory

<https://doi.org/10.1038/s41586-024-07107-7>

Sergey Bravyi<sup>1</sup>, Andrew W. Cross<sup>1</sup>, Jay M. Gambetta<sup>1</sup>, Dmitri Maslov<sup>1,✉</sup>, Patrick Rall<sup>2</sup> & Theodore J. Yoder<sup>1</sup>

Received: 25 August 2023

Accepted: 23 January 2024

## Constant-Overhead Fault-Tolerant Quantum Computation with Reconfigurable Atom Arrays

Qian Xu,<sup>1,\*</sup> J. Pablo Bonilla Ataide,<sup>2,\*</sup> Christopher A. Pattison,<sup>3</sup> Nithin Raveendran,<sup>4</sup> Dolev Bluvstein,<sup>2</sup> Jonathan Wurtz,<sup>5</sup> Bane Vasić,<sup>4</sup> Mikhail D. Lukin,<sup>2</sup> Liang Jiang,<sup>1,†</sup> and Hengyun Zhou<sup>2,5,‡</sup>

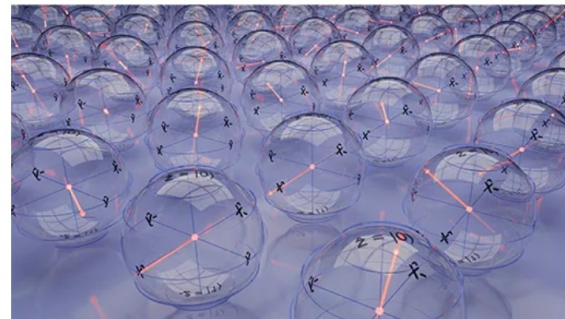
<sup>1</sup>Pritzker School of Molecular Engineering, The University of Chicago, Chicago 60637, USA

<sup>2</sup>Department of Physics, Harvard University, Cambridge, Massachusetts 02138, USA

<sup>3</sup>Institute for Quantum Information and Matter, California Institute of Technology, Pasadena, CA 91125

<sup>4</sup>Department of Electrical and Computer Engineering, University of Arizona, Tucson, AZ 85721, USA

<sup>5</sup>QuEra Computing Inc., 1284 Soldiers Field Road, Boston, MA, 02135, US



### QUANTUM COMPUTING

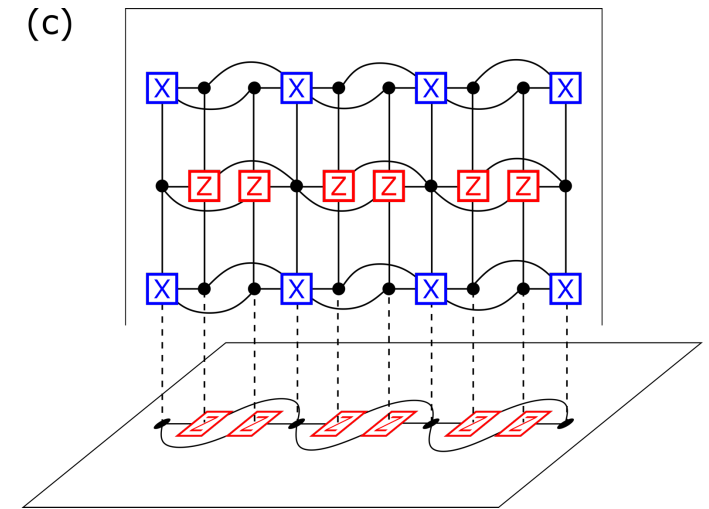
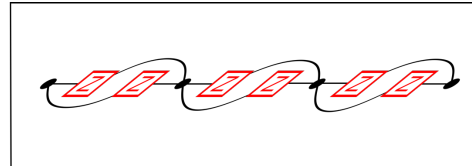
## New Codes Could Make Quantum Computing 10 Times More Efficient

By CHARLIE WOOD | AUGUST 25, 2023 | 6 |

Quantum computing is still really, really hard. But the rise of a powerful class of error-correcting codes suggests that the task might be slightly more feasible than many feared.

# qLDPC codes and FTQC – logic gates

- Still work to do to construct FTQC with LDPC codes including logic gates
- We have a new way of doing FT gates by generalizing **lattice surgery**



$k$	$d$	Parallelism	Code family	$n_{data}$	$n_{anc}$	$n_{tot}$
18	8	2	Hyperbicycle Surface	294	500	800
			Hyperbicycle Surface	1152	128	1300
50	14	2	Hyperbicycle Surface	900	1400	2300
	16	20	Hypergraph Surface	9800	300	10000
578	16	578	Hypergraph Surface	1922	5000	7000
			Hypergraph Surface	12800	2000	15000
	68	Hypergraph Surface	7938	120000	130000	
		Hypergraph Surface	150000	75000	225000	
578	16	68	Hypergraph Surface	7938	15000	23000
			Hypergraph Surface	150000	10000	160000

TABLE I. Estimates of the overhead required to perform a round of logic, including those qubits needed to encode the data as well as additional ancilla qubits required to perform fault-tolerant gates. We use LDPC codes constructed in [39, 40], which all have initial check weights of no more than 10. We denote the number of logical qubits as  $k$  and the distance of the code as  $d$ . Comparisons are made against the surface code with the same distance. Here, 'parallelism' denotes the number of logical qubits that can be acted upon non-trivially in one round of error correction, and which determines the number of required ancilla qubits. The number of data, ancillary, and total physical qubits needed to perform one round of logical measurements with error correction are denoted  $n_{data}$ ,  $n_{anc}$ , and  $n_{tot}$ , respectively. We do not include any ancilla qubits that may be used for error syndrome extraction.

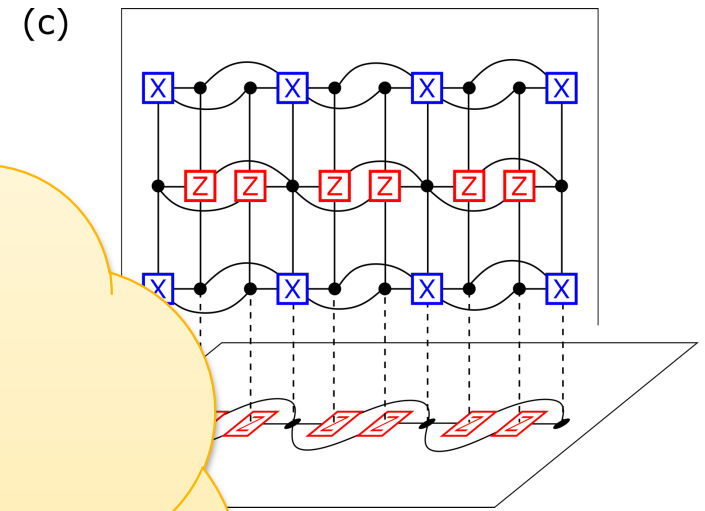
Cohen, Kim, Bartlett, Brown  
Science Advances 2022

# qLDPC codes and FTQC – logic gates

- Still work to do to construct FTQC with LDPC codes including logic gates
- We have a new way of doing FT generalizing **lattice surgery**

**Observations (qLDPC):**  
 Low-overhead architectures for FTQC based on qLDPC codes are within reach

Connectivity is front and centre; unlikely to find a good ‘once-size-fits-all’ architecture



				0
				500
				25000
578	1		10000	23000
			10000	160000

TABLE I. Estimates of the overhead to perform one round of logical operations, including those qubits needed to encode the data as well as additional ancilla qubits used for fault-tolerant gates. We use LDPC codes constructed in [39, 40], which all have initial check weights of  $n$ . We denote the number of logical qubits as  $k$  and the distance of the code as  $d$ . Comparisons are made against a code with the same distance. Here, ‘parallelism’ denotes the number of logical qubits that can be acted upon in one round of error correction, and which determines the number of required ancilla qubits. The number of ancilla qubits, and total physical qubits needed to perform one round of logical measurements with error correction are denoted as  $n_{anc}$ , and  $n_{tot}$ , respectively. We do not include any ancilla qubits that may be used for error syndrome extraction.

Cohen, Kim, Bartlett, Brown  
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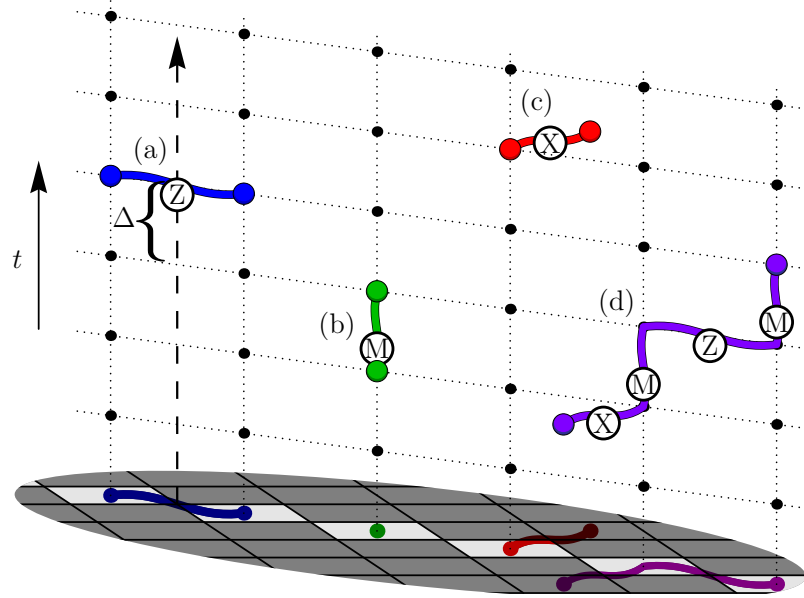


# Lowering the overheads 2

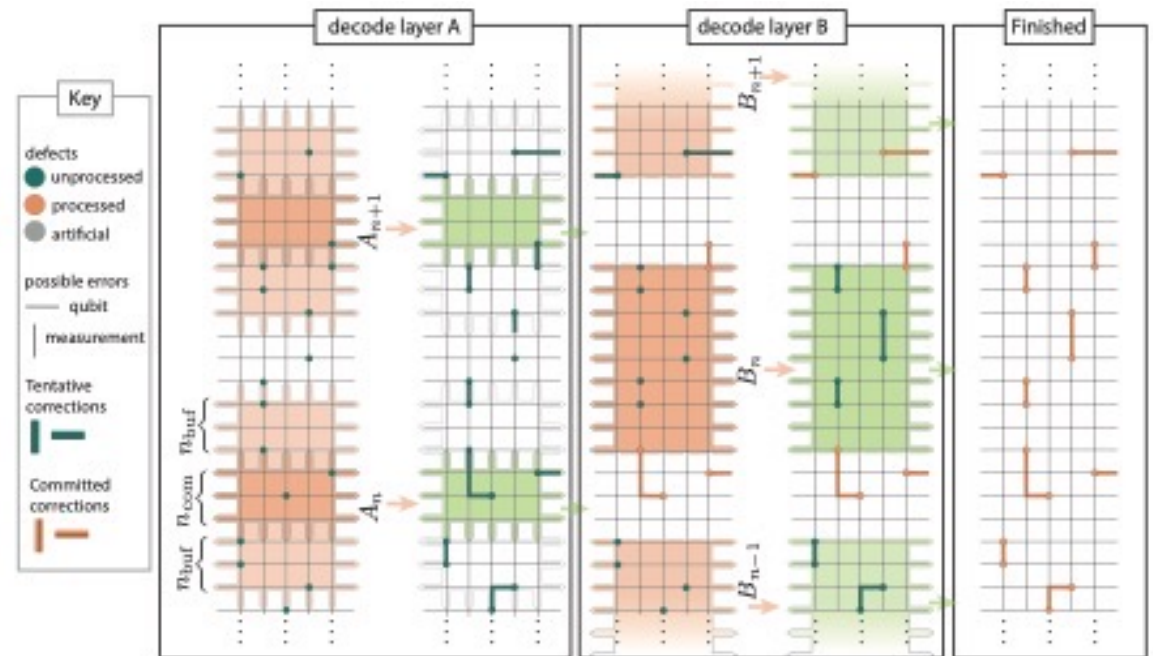
Don't waste my time

# Repeated syndrome measurements

- Surface code (and many others) require accurate syndrome measurements
- 'Standard' approach is to repeat syndrome extraction many ( $d$ ) times



Bonilla Ataides et al., Nature Comms 2021



Skoric et al., Nature Comms 2023

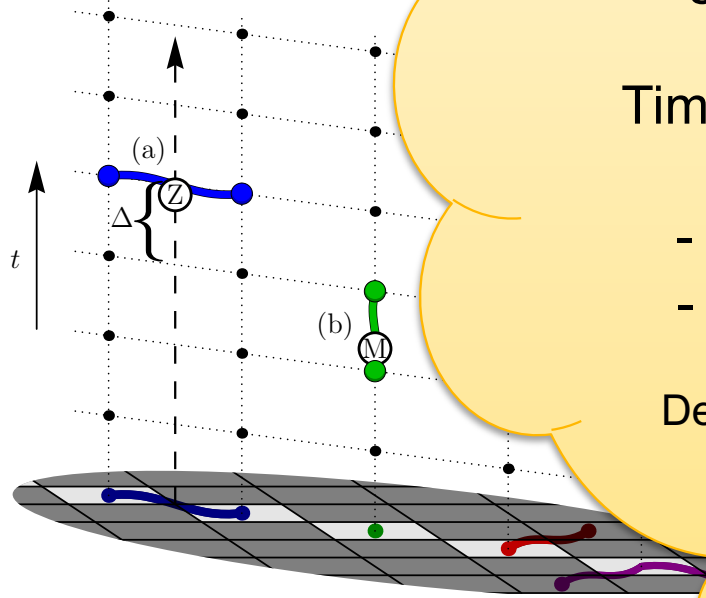
# Repeated syndrome measurements

- Surface code (and more)
- 'Standard' approach

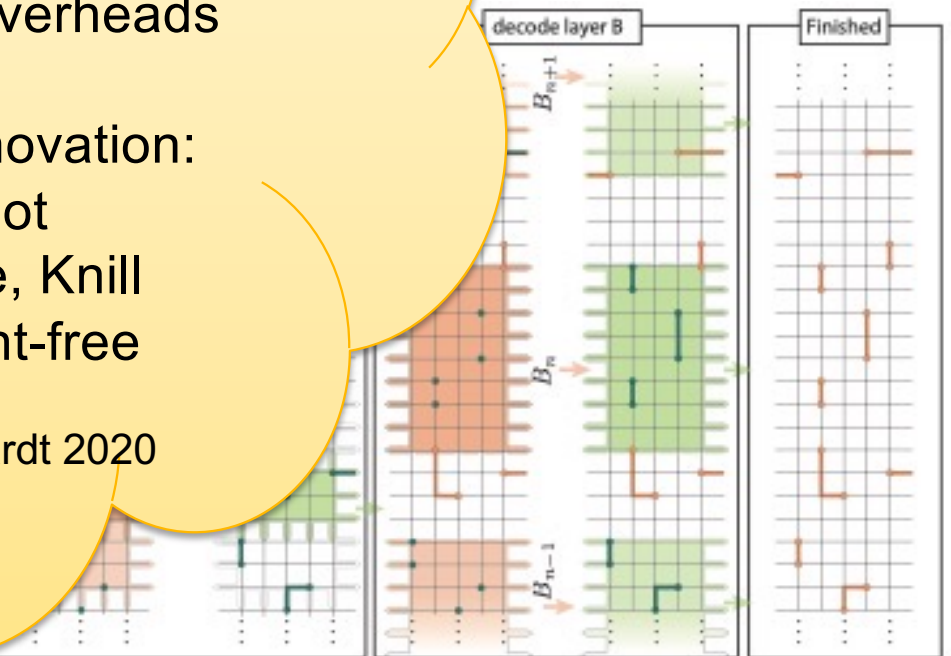
**Observations**  
**(FT syndrome extraction):**  
 Repeated measurements  
 brings large time overheads

- Time for some innovation:
- single shot
  - Shor, Steane, Knill
  - measurement-free

Delfosse and Reichardt 2020



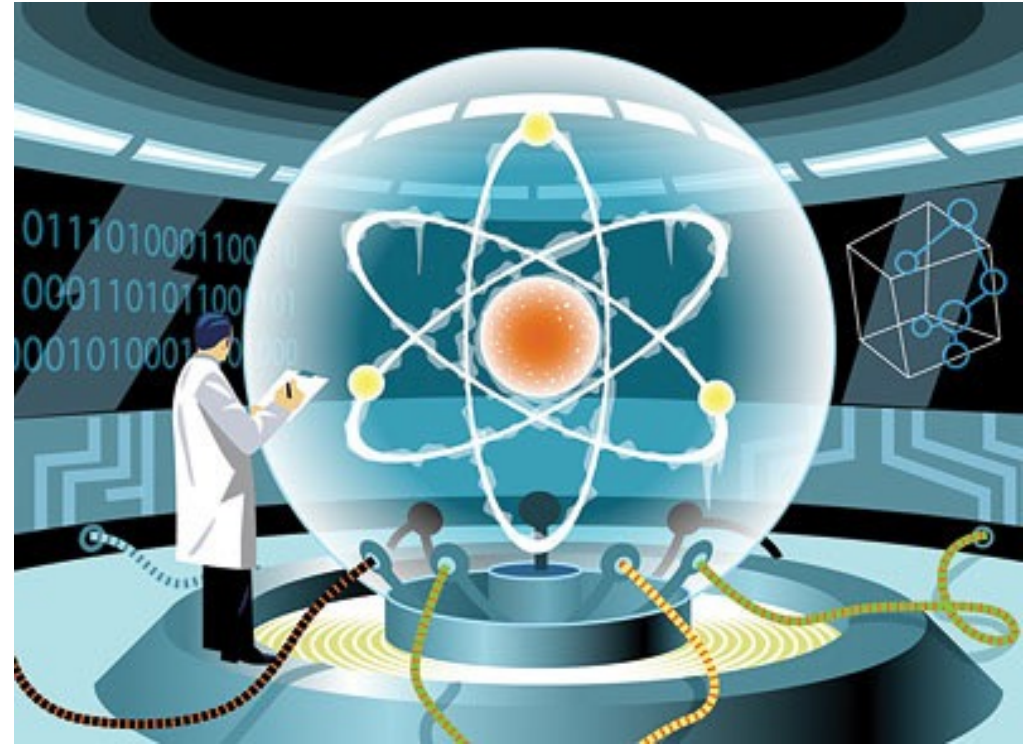
Bonilla Ataides et al., Nature Comms



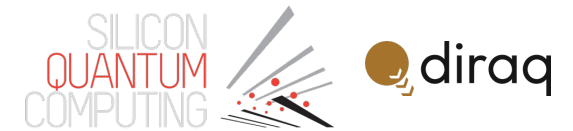
Skoric et al., Nature Comms 2023

## So where does that leave us?

- Quantum error correction will be incredibly challenging, but current estimates for resource overheads are likely pessimistic
- QEC is not a piece of quantum software to run, but a full-stack approach to integrate with hardware and control
- Plenty of opportunities for university-based researchers to innovate



# Sydney and quantum

The logo for the Sydney Quantum Academy, featuring a stylized red and orange atom-like structure and the text "SYDNEY QUANTUM ACADEMY".

\$35M for training and entrepreneurs

The logo for the state of New South Wales (NSW), featuring a red lotus flower and the text "NSW" in blue.

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*A Physical Review journal*

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